

A review of contact algorithms

N. G. Bourago and V. N. Kukudzhanov

The Institute for problems in mechanics of RAS, Moscow, burago@ipmnet.ru

Izv. RAN, MTT, No. 1, pp. 45–87, 2005.

translation into english

A review of contact algorithms ¹

N. G. Bourago and V. N. Kukudzhyanov

The Institute for problems in mechanics of RAS, Moscow, burago@ipmnet.ru

Moving interfaces between media play an important role in technological and natural processes. The development of methods for solving problems with moving interfaces is one of the major aims of continuum mechanics. This review concentrates on parts of the numerical methods of continuum mechanics named contact algorithms that serve to track and calculate moving interfaces such as contact, phase change, and moving free boundaries.

1. Types of contact algorithms under consideration

Contact algorithms can be classified according to the concept utilized for the description of motion of a continuous medium. In Lagrangian contact algorithms, the nodes move with the velocity of the material medium. In non-Lagrangian contact algorithms, the nodes either are fixed (Eulerian algorithms) or move independently of the material medium (Arbitrary Lagrangian–Eulerian (ALE) algorithms). A characteristic feature of non-Lagrangian algorithms is the occurrence of convective terms in the evolution equations due to a difference in the velocities of the grid (coordinate system) and the medium.

In both cases (Eulerian and Lagrangian), the moving interfaces can be treated explicitly by *tracking algorithms* as a set of surface nodes (or markers) and cells or be defined implicitly by *capturing algorithms*. The capturing algorithms are based on continuous marker functions that take on a certain constant values at the moving boundaries.

This known classification underlies the systematization of the publications to be reviewed. In the present paper, we consider all types of contact algorithms, irrespective of the types of contacting media, which is in agreement with the modern tendency to unify the methods of solid mechanics and hydrodynamics. This tendency is accounted for by the requirement for construction of unified computational models for technological and natural processes.

2. Types of boundaries under consideration

In addition to the classical initial-boundary value problems of continuum mechanics, the contact problems involve specific boundary conditions (kinematic and dynamic constraints, phase change laws) that govern the motion of the interfaces and possible boundary singularities.

For the classical contact problems, such conditions express the impenetrability constraint, the action-reaction law (Newton’s third law), and the surface friction law. The normal contact constraints prevent mutual penetration of immiscible media, while the tangent contact constraints represent friction between the contacting media. The extended physical-chemical formulation involves also boundary conditions for heat transfer, electromagnetic interaction, diffusion, chemical reactions, etc.

Additional relevant cases of boundary conditions determining the behavior of free and phase change boundaries are also considered. The moving free boundaries are Lagrangian surfaces between a condensed (liquid or solid) medium and a rarefied medium. The boundary conditions at the free boundaries describe the influence of the rarefied medium characterized by the forces of external pressure and friction, as well as the surface tension forces, which depend on the orientation and the curvature of the boundary (besides the dependence on state variables).

Unlike the classical contact and free boundaries, the phase change boundaries are non-Lagrangian, and the motion of such boundaries in a continuum is governed by the phase equilibrium conditions (such as, for example, Stephan’s law, Chapman–Jougeot detonation condition, yield condition, fracture condition, etc.) The phase change boundaries are weak discontinuity surfaces that move along the continuous medium tracking the phase change process characterized by sharp changes in the properties of the continuum. The temperature, velocities, displacements, and stresses are continuous at the phase change boundaries, whereas the coefficients of elasticity and plasticity, heat capacity, compressibility, and other media properties can undergo a jump discontinuity.

One more important special limiting case of contact is a contact of deformable solid and liquid media with rigid bodies. This type of contact is also considered in the present review.

¹ N. G. Bourago and V. N. Kukudzhyanov, “A review of contact algorithms,” *Izv. RAN, MTT*, No. 1, pp. 45–87, 2005.

3. Reviews of formulations of contact problems

Initial-boundary value problems can be formulated in the differential, integral or variational forms. The variational formulations, especially the formulations in terms of variational inequalities, play an important role in the analysis of the existence and uniqueness of solutions of initial-boundary value problems and their well-posedness.

Formulations of contact problems have been dealt with in [136, 156, 170, 193, 369–371, 410, 423, 501, 503, 544, 545, 556, 557], where one can find references to additional sources. Theoretical foundations for the statement of contact problems related to phase changes have been reviewed in [76, 199, 299, 351, 420, 421, 428, 524]. Bibliographic lists of publications devoted to the existence and uniqueness of solutions of contact problems can be found in book of collected reviews [587].

In many of the modern publications on contacts of media the initial-boundary value problems are formulated in the Galerkin variational form. In this case, the boundary conditions are treated as constraints to be taken into account in the variational equation by using Lagrange multipliers or penalty functions. For a review of methods to take into account constraints in general variational problems, see, for example [497].

A reviews of Arbitrary Lagrangian-Eulerian formulations of continuum mechanics problems are given in [63, 89, 165, 214, 282, 299, 361].

4. Reviews of methods for contact calculations.

A large number of recent reviews of numerical-analytical methods for contact calculations, initiated by Hertz's work [275], are given in the book of collected reviews [587].

In the present paper, we consider numerical-discrete methods for the calculation of contact boundaries. These methods comprise finite-difference, finite-volume, and finite-element algorithms, as well as Galerkin's "meshless" methods and contact algorithms of the boundary element method.

Large bibliographies on contact algorithms in solid mechanics have been presented in [6, 76, 99, 199, 232, 233, 289, 331, 374, 397, 625, 627] and in a number of other publications cited in what follows farther in connection with algorithms of specific types.

Reviews of algorithms for calculating the interfaces of immiscible media within the hydrodynamics framework are presented in [11, 12, 58–60, 76, 214, 315, 359, 360, 494, 509, 538].

5. Lagrangian algorithms for calculating contacts with rigid bodies.

An overwhelming number of publications on contact problems relates to contact of deformable solid and liquid media with rigid bodies (walls, punches, impactors or obstacles). In this case, the moving boundary of rigid bodies is regarded as a prescribed slip surface. This surface can be smooth or rough. The motion of the rigid bodies is either assumed to be predetermined or calculated by using the methods of theoretical mechanics taking into account the mass of the rigid bodies and the contact reaction forces.

Examples of calculations for contacts with rigid bodies, as well as additional references, can be found in [31–33, 198, 248, 344, 346–348, 374, 431, 485, 495, 616, 617]. Reviews of investigations in this direction are given in [150, 199, 550]. In Lagrangian contact algorithms, the velocities at the boundaries between rigid and deformable media are either prescribed or determined by the penetration of the nodes of the moving grid in deformable media into the prohibited spatial regions that represent rigid bodies. The velocity and displacement components normal to the surface of the rigid body are corrected to prevent the penetration. In many algorithms, such a correction is reduced to the equating of normal velocities of the deformable and rigid boundaries. The correction can be also performed by the elimination of the penetration by applying external normal loads, which represent the contact pressure. The calculation of friction forces does not have specific features in comparison with more general contact algorithms and is considered farther.

6. Lagrangian capturing contact algorithms.

In the Lagrangian capturing algorithms, the solution is continuous at the contact boundary and contact discontinuities are modeled by large gradients of the solution.

Models of ideal contact. Matched grids. A simple approach to the calculation of a contact in the case of small strains for a prescribed (possibly moving) Lagrangian contact boundary involves an approximate representation of the full adhesion conditions that characterize the ideal contact. The Lagrangian grids in the contact region are matched node to node, slip and rebound (coming unstuck) of the contacting bodies are prohibited. The solution at the contact boundary is continuous for the displacement and velocity (ideal contact). There are many publications in which such a scheme is used for contact calculations. Any algorithm for solving continuum mechanics problems by a grid based method can serve as an example. If

different properties of the material have been prescribed in different domains, such an algorithm implements the conditions of ideal contact automatically.

Typical examples of calculations for the ideal contact can be found, for instance, in old Russian papers on finite-element method published 20-30 years ago [382, 440, 491, 493, 514, 515, 542, 582, 586]. For references to international publications on the ideal contact, see, e.g., [632].

In the general case of variable contact region, where the slip and coming unstuck of the contacting bodies can occur, the ideal contact model, which ignores these phenomena, is physically inadequate and, therefore, is not utilized.

Ideal contact. Unmatched grids. A contact algorithm for matching the solutions to satisfy the ideal contact conditions in the case of unmatched grids in the contact region has been proposed in [47] for 2D case and developed in [49, 50] for 3D case. Apart from the contact calculations, this algorithm is utilized for the calculation of joints in composite structures. This algorithm does not require one to worry about the matching of the grids at the boundaries of subdomains to provide continuity of the solutions. This simplifies the construction of grids in combined 3D subdomains of complex shape. Recently these algorithms have been rediscovered [191, 477, 479].

Buffer layer algorithms are based on the introduction of a fictitious buffer contact layer (contact pseudomedium) between the contacting bodies. The buffer layer consists of the contact cells, the nodes of which belong to the contacting boundaries. The introduction of the buffer layer of cells reduces the contact problem for many bodies to a problem for a single composite inhomogeneous body. As a rule, only one cell is utilized across the buffer layer thickness. Depending of the prescribed properties of the contact, these cells can play the role of an elastic spring, a viscous damper, an adhesive contact, etc. The stresses acting in the buffer layer imitate the contact loads. The success or failure of this imitation depends on the properties prescribed for the material of the buffer layer. These properties should provide the appearance of compressive contact loads, prevent the appearance of tensile contact loads (to model coming unstuck), and model friction forces. The resulting mathematical model should be well-posed. In addition, for “cosmetic” and accuracy reasons, the buffer layer thickness is desired to be much smaller than the characteristic size of the contacting bodies.

The issues of the implementation and theoretical substantiation of the buffer layer algorithms have been considered, for example, in [155, 211, 362, 381, 430, 433, 447, 448, 480, 492, 516, 518, 519, 555, 588, 619–621].

Lagrangian united-equation-of-state algorithms serve for the calculation of the development of internal contact discontinuities such as macro-cracks. In these algorithms, cracks are modeled by narrow internal zones with weakened resistance of the material to deformation. These zones are formed if some damage criterion has been satisfied. For the description of such through calculation algorithms, see, e.g., [65, 66, 87, 88, 96–98, 100, 199, 253, 254, 300, 312, 349–351, 374–376, 404, 405, 416, 442, 457, 527, 576]. If the damage criterion (for example, formulated in terms of the limiting principal strains or stresses) has been satisfied in a Lagrangian cell, the elastic moduli and stresses relax to zero forcing strain localization and only the compression strength is preserved in the material. A comprehensive review and the description of this type of through calculation algorithms is given in [199]. It can be easily seen that the narrow damage zones in such algorithms are similar to the buffer contact layers that have been considered previously.

Multiple contact. Problems of multiple contact of deformable bodies appear in many applications, for example, in the numerical study of the properties of composite materials consisting of many contacting components, in the calculations associated with hitting a target with a case-shot or in the analysis of the interaction between rough surfaces. Publications in this direction have been reviewed in [199, 220, 235, 363, 599, 602, 609].

Algorithms for calculating multiple contact in accreting bodies have been considered in [16, 420, 421]. This type of problems covers the layer-by-layer formation of composite materials, loading of a soil during the construction work, growth of crystals in the process of solidification of metallic melts and polymer solutions, spraying, deposition, and freezing.

When solving multiple contact problems, helpful are the models and algorithms for through calculation of contact boundaries that have been utilized for studying the strength properties of composite materials by considering the deformation of an idealized small domain containing a fairly large number of dissimilar contacting subdomains (the matrix and inclusions).

As the number of the contacting elements increases, the direct numerical modeling becomes complicated and one has to involve continuum models for the multiple contact. For example, an effective method for solv-

ing multiple contact problems for sandwich and block structures is based on the asymptotic homogenization for media with periodic structure. A review of publications in this direction is given in [446], with particular cases of homogenization models and their numerical implementation being presented. The approach developed in the cited publication allows effective modeling of fracture in masonry structures, a brickwork or layered rock, with delamination and friction on contact surfaces being taken into account. The constitutive relations for these structures are similar to those for an elastoviscoplastic medium. The delamination is taken into account by specific functions.

The modeling of non-Lagrangian interfacial boundaries (e.g., liquid–vapor or liquid–solid for melting or crystallization)[531, 538] on the basis of united-equation-of-state algorithms will be considered below when describing Eulerian through calculation contact algorithms.

7. Contact detection algorithms.

For the numerical calculations on the basis of Lagrangian grid methods, the boundaries of bodies are represented by a set of boundary surface cells. In most cases, the contact region is unknown in advance and has to be detected during the calculation. It is identified either by the penetration of “alien” boundary nodes through “friendly” boundary cells in the preliminary calculation, in which the contact is not taken into account, or by the approach of the boundaries to a prescribed small distance which the fact is detected by the pairwise check of the mutual positions of boundary nodes and cells. The search for the contact region results in a list of contact pairs (for example, of the “alien node–friendly cell” type), which introduce the contact or buffer elements. Sometimes, the contact pairs can be represented by combinations of “node–fictitious node” or “cell–cell”, i.e., by pairs of discrete elements of the contacting boundaries.

The number of operations for searching for contact pairs is proportional to the square of the number of boundary cells or nodes. For problems with large number of nodes this leads to unacceptably great computational effort. Farther, we consider available algorithms for accelerated search for the contact region.

Master–slave (node-to-segment) algorithm is one of the first contact searching (detection) algorithms. It was proposed in [238, 260]. To reduce the computational effort, the regions of possible contact are specified in advance. One of the contacting surfaces is considered to be the master surface and the other (slave surface) is subordinated to it. The master surface is represented by the boundary cells and the slave surface by the boundary nodes. The algorithm utilizes a priori information about the region of possible contact and identifies contact pairs by the penetration of the slave nodes through the master’s boundary cells. To detect the penetration, the algorithm checks the sign of the normal projection of the slave node onto the master cell and the fact that the normal dropped from this node onto the cell intersects this cell.

Note that in many problems, it is impossible to predict master and slave contact surfaces in advance. The necessity to describe the contact regions in the initial data for bodies of complicated geometry is rather burdensome. An additional argument against the utilization of a priori information about the contact region is the possibility of self-contact. By self-contact, the contact between different parts of the surface of the same body is understood. Self-contact can occur in the case of large deformation.

In the contact searching algorithms to be considered in what follows, the search process is divided into two or more levels to accelerate the process of detection of contact pairs. These levels are usually referred to as the global and local ones. On the global levels, the regions of possible contact are searched for among groups of neighboring nodes. The groups of nodes that lie far away from the region of possible contact and, therefore, are not involved in contact are rapidly discarded in accordance with an appropriate group criterion associated with the distance. On the last (local) level, contact pairs “node–boundary cell” are identified by the violation of the impenetrability constraint or by a sufficient proximity criterion. The contact searching algorithms differ from one another in the criteria for grouping the nodes, group characteristics, hierarchy, and methods for quick sorting.

Among the well known global algorithms of searching for contact region, we mention the regular cell algorithm [530], the hierarchy–territory algorithm [626, 628], the linear position code algorithm [623, 624], the bucket sorting algorithms [64, 75], and the spherical sorting algorithm [472].

The hierarchy–territory algorithm and the linear position code algorithm are most widely utilized and efficient global contact searching algorithms.

The *Hierarchy–Territory Algorithm* (HITA) [626] is based on the grouping of the boundary elements lying close to one another and searching for possible contact regions by means of the analysis of the distances between the groups of elements. After having found possible contact groups, the local search is performed.

If the number of the boundary elements is very large, a hierarchy of the groups is constructed and the search for a possible contact occurs consecutively from higher-level to lower-level groups.

The *Linear Position Code Algorithm* (LPOCA) [455] artificially orders all boundary nodes of the finite-element grid. To that end, the parallelepiped bordering the solution domain is divided into a large number of small “bricks” with a structured ijk numbering, i.e., an additional uniform regular ijk grid is introduced. Each node of the unstructured finite-element grid is assigned an ijk number, depending on the small “brick” entered by this node. Such an additional numbering contains information about the arrangement of the nodes, which enables one to use this numbering for forming clusters (groups of neighboring nodes) and reducing the number of checks, thereby accelerating the search for contact regions (see also [21, 273, 418, 419]).

The *Space Filling Curve* algorithm (SFC) [157] hierarchically divides the solution region into squares as is the case in the familiar problem of catching a lion in Sahara desert. Parts of the desert are consecutively bisected with the selection of the part in which the lion is located. The bisection continues until the current part becomes so small that the lion has no place to hide. In a similar way, the SFC algorithm divides the searching domain into four rectangular parts (in the 2D case) until only one node remains in the cell. This node is assigned a position code (an address) formed by a chain of binary codes (00 for the left lower part, 01 for the right lower part, 10 for the left upper part, and 11 for the right upper part) to indicate the path to the given node. To detect the neighbouring nodes for the given one, the algorithms of quick comparison of position codes are utilized. These algorithms are based on XOR-operations combined with binary and exponential search.

The local *inside-outside algorithm* [590] effectively copes with the “deadzone” problem. The matter is that at the inflections of the boundary there appear internal dead zones and it is unclear where the alien boundary node penetrated the boundary and situated in the dead zone could be “pushed out”. The algorithm suggests a simple strategy, according to which this node should be pushed out backward by means of the reaction forces directed along the Lagrangian trajectory of the node (inside and outside in the same track).

The local *gap function algorithm* (GFA) [280], according to the concept of its authors, should enable all contacts for problems characterized by very complicated geometry and very high dimension to be considered in a unified way. The algorithm is based on the scalar gap (material depth) function defined in the domain of the solution. For each node, this function is calculated one time for the initial position of the moving boundary and is equal to the initial distance from this node to the nearest boundary. Outside the solution domain this function takes on zero value. Penetrated alien node lies inside some cell of the spatial grid and, hence, is characterized by two values of the gap function. One of these values (the proper value for this node) is equal to zero, while the other one corresponds to the position of the node inside the cell and is nonzero. The direction of push back contact forces is defined by the negative of the gap function gradient; the penetration depth and reaction force magnitude are proportional to the gap function value. The efficiency of the gap function algorithm depends on the efficiency of the interpolation of the gap function.

The gap function approach is criticized in [470]. According to this study, preferred are conventional contact pair algorithms, which fit better to the general case of nonsmooth boundaries with inflections and the case of multiple contact.

The local *pinball algorithm* [68, 69] has been proposed to identify complex cases of contact of dissimilar elements (rods, shells, and spatial members). This method considers a spherical neighborhood of each element irrespective of its nature (3D, 2D shell, or 1D rod/beam) and contact detection is simplified to an interference check between these bounding spheres. This procedure is simple, since contact takes place if current distance between centers of pinballs is less than the sum of their radii. Push back contact forces are applied to the centers of the overlapped pinballs. The magnitude of push back forces is proportional to the overlap measure. Then these forces are recalculated from pinball centers to the nodes of the elements to which these pinballs are related. Since the pinball algorithm is based on simple checks, this algorithm is very quick. It spends about 15% of time required for the calculation of one time step, while other algorithms sometimes spend more than 65–70% [76].

The *hierarchical pinball algorithm* has been developed to remove the drawbacks of the pinball method. These drawbacks were indicated in the paper [69], in which the pinball method was utilized for thin shells. It turned out that the pinball method failed if the contacting elements were very thin. To overcome this difficulty, two modifications of the pinball algorithm have been proposed—the quick pinball algorithm and the splitting pinball algorithm [70]. As is the case for the conventional pinball algorithms, in the splitting

algorithm, a pinball is associated with each element, although in the modified method the radius of the pinball is always chosen to be large enough to surround the element. This large pinball is referred to as the parent one. The overlap of the parent pinballs indicates only the possibility of the penetration. If the overlap of the parent pinballs has been identified, smaller lower-level pinballs are arranged. The radii of these pinballs coincide in order of magnitude with the thickness of the shell. The smaller pinballs, distanced by this radius from one another, cover the surface of a shell element or the length of a beam element. The overlap of the smaller pinballs with alien pinballs indicates the penetration. In this case, the desired contact forces are calculated in accordance with the overlap of the small pinballs and then are recalculated for the nodes of the corresponding surface grid elements.

In a frame of meshfree Galerkin methods an effective *meshfree contact algorithm* based on the principle of moment of meshfree interpolation is proposed in [459] (see also [57, 458]).

8. Lagrangian contact algorithms. Calculation of contact forces and velocities.

Let the contact region has been identified and let the node–cell contact pairs have been constructed. Consider algorithms for calculation of the contact velocities and forces.

Slip contact algorithms have been proposed in pioneering works by M. Wilkins [511, 593–598] on the contact between deformable bodies in the case of variable contact region. The works by M. Wilkins have greatly influenced the development of the contact algorithms for the case of large deformation.

In the slip algorithms, at each time instant, one of the contacting surfaces (alternately) is regarded as the slip surface (a surface of a rigid body), while the other surface follows the motion of the first one [332–334]. Although the contact conditions in this case are satisfied approximately, on the average, this method provides plausible results. The contact forces and velocities in the numerical solution obtained by means of this method oscillate, which reduces the accuracy of the computation.

For the extension of Wilkins method to 3D case, see, for example [48, 248, 310, 311, 313, 352, 353].

Fictitious node contact algorithms have been introduced in various forms in a number of publications. In the paper [47], which has already been mentioned in connection with ideal contact algorithms, a 2D algorithm utilizing the impenetrability constraint along the normal and the free slip condition along the tangent has been proposed. In the case of mismatch of the grids in the contact region, this algorithm uses an auxiliary matched grid that consists of the boundary nodes of the primary grid in one of the bodies and the corresponding (having the same position) fictitious boundary nodes in the other body. The values of the solution at the fictitious nodes on the old time layer (iteration) should be determined by means of interpolation. On the new time layer, each pair of adjacent (primary–fictitious) boundary nodes is subjected to the kinematic constraint (equality of the corresponding normal velocity components) and the static condition (equality in magnitude of the normal force components). These relations are utilized to determine the contact pressure magnitudes and correct the boundary nodal velocities at each boundary node of the primary grid. This algorithm has been extended to 3D contact problems in [50].

Fictitious nodes have been introduced also in many other contact algorithms, for example, in the characteristic algorithms [617] to be considered below and in the hierarchical pinball algorithm [69] that has been considered previously.

A logical completion of the line of fictitious-node algorithms is provided by the adaptive contact algorithms. These algorithms at each time step reconstruct the grids locally in the contacting bodies in the neighborhood of the contact region to provide the node-to-node match of these grids [434].

Characteristic contact algorithms. The relations on the characteristics for hyperbolic systems of equations of mechanics of elastoplastic media have been utilized in [347, 348, 485, 617] for the calculation of contact boundaries in 2D problems. The systems of characteristic relations have been written out for each boundary node in one body and the corresponding fictitious node in the other body. The solutions of these systems of equations have been used to determine the contact velocities and forces. The characteristic algorithms can be applied only to unsteady hyperbolic problems. For an update review of the characteristic algorithms, see, for example, [378].

Contact algorithms based on the Riemann problem and Godunov scheme. The Godunov scheme [223] utilizes the solution of the Riemann problem for the decay of an arbitrary discontinuity. It has been applied by Godunov with co-authors [225] to the calculation of contact interactions in the explosion welding processes. In [225], one can find the description of the contact algorithm and references to other publications of the authors. This line of algorithms has been developed in [1, 9, 10, 520–524]. The family of Godunov algorithms

has been described in the review of [76] and monographs [378, 578].

Inelastic impact contact algorithms have been applied in various modifications in [19, 243, 244, 296, 297, 354, 525, 526, 533]. In these algorithms, the velocities of the Lagrangian nodes in the impact contact region are corrected on the basis of the solution of the problem of an inelastic impact for the nodal masses that form node–surface cell or node–fictitious node contact pairs.

Contact algorithms based on Lagrange multipliers take into account the desired normal contact loads in the virtual work principle or in discrete equations of the contact nodes motion taking into account the impenetrability constraint. The normal contact loads in this formulation are the Lagrange multipliers for the impenetrability constraints. The difference between various modifications of this approach can consist, for example, in the form (continuous or discrete) in which the impenetrability constraints are taken into account, in the methods (direct or iterative) utilized for solving the system of algebraic equations for the nodal contact pressures, in the interpretation (physical or mathematical) of the algorithms, and in the methods of approximation of the solution in the contact region. However, despite the apparent differences, all these modifications are various versions of the realization of the same concept. Note that most of the contact algorithms applied in explicit computational schemes can be regarded as versions of the Lagrange multiplier method.

For small deformations, the algorithms based on Lagrange multipliers have been constructed in [204, 256, 286] - [262], [17], [39–41, 245, 399]. For large deformations such algorithms have been developed in [50, 90, 91, 93, 95, 109, 113, 228, 230, 251, 355, 357, 473, 507, 529, 546, 547, 551, 623, 624, 628].

Penalty function algorithms provide another version of dynamic contact algorithms applied most frequently in implicit schemes to solve contact problems in quasi-static and dynamic formulations. In these algorithms, the normal load magnitude is assumed to be proportional to the residual of the impenetrability constraints with large coefficients of proportionality (penalty coefficients).

Contact penalty function algorithms for implicit schemes have been developed and described in [18, 44, 93, 95, 111, 119, 202, 245, 258, 291, 325, 329, 331, 356, 377, 409, 450, 451, 474, 488, 546, 608, 609, 626].

The hybrid algorithms, which combine the penalty function and Lagrange multiplier methods, have been also developed; see, for example [43, 181, 182, 272, 388, 401, 548, 600, 608, 609, 618].

Lagrangian algorithms for explicit treatment of internal contact boundaries. An alternative to the through calculations algorithms for main cracks is an approach to the fracture modeling in which contact discontinuities corresponding to main cracks are determined explicitly [82, 129, 293, 440, 517]. In this approach the contact surface is introduced in advance and is defined by paired nodes. In the general case, additional nodes are introduced in the process of solution [244, 432]. Algorithms for reconstructing the grids in the neighborhood of contact discontinuities are reviewed and described in [214, 384, 385].

A method for explicit treatment of newly formed contact discontinuities, based on the local reconstruction of the grid by means of “collapse” of the destroyed cell (by means of shifting the nodes of this cell onto the fracture surface), has been proposed and described in [199, 250, 335]. This method does not require introducing new nodes.

In a number of algorithms, crack-type discontinuities are modeled on the level of elements without reconstruction of the grid [549, 559], by using the moving ALE grid technique [506], as well as by introducing additional degrees of freedom in the elements containing a contact discontinuity [149, 162, 163, 169, 194, 196, 437]. These additional degrees of freedom are associated with specific shape functions.

9. Eulerian algorithms for calculating contact boundaries.

Let us imagine the case where two or more domains occupied by one phase of the material coalesce (e.g., merging liquid drops). It is difficult to model such a process by means of Lagrangian grid methods with explicit treatment of interfaces. This is especially difficult in the case of 3D problems, since the combination of nodes into Lagrangian boundary cells is defined by lists, and these lists would have had to be continuously updated. Additional difficulties would have arisen because of unacceptable Courant’s restrictions for the time step in the case of too close approach of the Lagrangian nodes. Similar difficulties are characteristic of the Lagrangian approach when applied to the modeling of fragmentation processes (for example, separation of a liquid drop).

These difficulties in tracking the interfacial boundaries can be overcome by utilizing Eulerian and Eulerian-Lagrangian front-tracking algorithms. In the broad interpretation of this review, these algorithms are treated as contact algorithms.

Reviews of Eulerian front-tracking algorithms. Eulerian methods for through calculation of contact discontinuity form a specific rich world of algorithms and deserve a separate review. In the present review, these methods are described briefly. Other bibliographies of publications on the Eulerian contact algorithms can be found, for example, in [59, 76, 151, 152, 189, 214, 292, 358, 460, 462, 463, 494, 536, 537, 564, 584].

Characteristic of this group of contact algorithms is that the calculation is performed on an Eulerian (fixed) grid (often uniform and rectangular), which contains the contacting material bodies and media with margin, and that the contact boundaries (common boundaries of media and bodies, free boundaries, and phase change boundaries) are tracked by means of Lagrangian discrete or continuous markers. Sometimes, an Eulerian-Lagrangian arbitrary moving (dynamically adaptive) grid is utilized instead of an Eulerian grid.

The velocity field calculated on an Eulerian grid is utilized for calculating the motion of discrete or continuous Lagrangian markers on the basis of the transport equations in the Lagrangian (for discrete markers) or Eulerian (for continuous markers) form.

Discrete Lagrangian marker algorithms form a large family that involves the basis algorithms for the particle-in-cell method [266], the boundary marker method [449], and the marker-and-cell method [436, 443, 574, 575, 591]. In these algorithms, mass, momentum, and energy is transported by particles, while the markers serve for the identification of the interfaces and the motion of the phases.

Cited above marker-and-cell algorithms deal with fluid-fluid interactions and free boundary motion. Versions of the marker-and-cell method for contact of elastoplastic bodies are presented in [199, 322].

In the case of discrete particle and marker methods when dealing with complex boundary conditions (e.g., friction, surface tension, and phase change), one has to use boundary Lagrangian cells to determine the geometry of contact (interfacial and free) boundaries. The boundary Lagrangian cells enable one to calculate normals, tangents, and curvatures of the interfacial surface to formulate the boundary conditions. As was the case for purely Lagrangian grid algorithms, such a Lagrangian description of the boundaries encounters considerable difficulties when identifying disappearing or arising boundaries. Therefore, the particle and marker methods are good while simple boundary conditions (which do not require calculating the geometrical characteristics of the contact boundary) can be utilized.

Besides, the particle and marker methods strike with problems of correct description of the boundary markers motion, problems of maintenance of conservation laws near boundaries, problems of insufficient number of markers or particles in rarefaction regions and problems of the generation and removal of markers at open boundaries. These problems can be solved in principle, but complication of the algorithms can lead to an unacceptably large number of operations.

Continuous Lagrangian marker methods enable one to simplify the description of boundary conditions and physical phenomena at the contact boundaries and the identification of these boundaries. This is especially important in the cases of variable topology of the subdomains occupied by various phases, when the phases merge or separate. The type of the medium is identified by the values of functions of continuous Lagrangian markers that remain constant along Lagrangian trajectories. These functions obey Eulerian transport equations. The interfacial boundaries are defined as an equal level surfaces of the marker functions. The same method for describing boundaries has been adopted, for example, for describing coast lines in cartography.

Various versions of continuous Lagrangian marker algorithms based on the continuous marker concept are presented in a number of publications, some of which are cited below.

The *large particle method* has been applied for interfacial boundary tracking in [103, 104, 283]. In these publications, the boundaries between the heavier and lighter media are identified by the level surface of the density.

In the *volume-of-fluid method* [103, 104, 283, 424], *pseudo-concentration method* [572], and *scalar equation method* [318], interfacial boundaries are identified by the level surfaces of the volume concentrations or “color” functions of various media.

In *level set methods* [174, 380, 461, 463, 464, 536–539, 561, 562], the interfaces are tracked by the level function that indicates the distance to the interfacial boundary.

The idea of boundary tracking based on the concentration or domain function has been described also in publications on the through calculation of the boundaries [176, 456, 531], fictitious domain method [108], and R-function method [492, 519].

The method of continuous markers that take on certain constant values for each of the contacting media

(i.e., have a shape of the Heaviside step function) suffers from interface blurring due to numerical diffusion. The zone of jump change of the continuous marker function from one value to another at the interface gradually increases, which is accounted for by errors in the numerical solution of the Eulerian transport equation for the continuous marker.

This difficulty is not encountered in the level set method applied to a slowly changing marker function based on the distance to the interfacial boundary, since the accuracy of the solution of the Eulerian transport equations for this slowly changing function is much higher.

Nevertheless, conservation laws are violated near the interfacial boundary for all marker (discrete and continuous) methods and, therefore, some additional techniques to control and correct the solution are necessary [219].

As compared with particle methods and discrete marker methods, continuous marker algorithms enable one to calculate normals, tangents, and curvatures of the contact surface in terms of derivatives of level function in Eulerian cells containing the boundary surface, thereby simplifying the computational procedure. The corresponding mathematical expressions for the geometrical characteristics can be utilized in boundary conditions on contact interfaces. These boundary conditions can express, for example, Stephan's law, or force conditions for pressure, friction, and surface tension.

In many cases, marker methods solve problems that have failed to be solved by methods implying explicit description of contact boundaries. This is the case, for example, for multiple contact or phenomena with variable topology of material subdomains (e.g., breaking waves, fountains, fragmentation of bodies during fracture, drop separation or merging, filling reservoirs, bubbles, and cavitations).

Eulerian methods for through calculation of a contact are especially efficient for transient processes, in which case the errors that violate conservation laws and blur boundaries do not have enough time to become noticeable. This is the case, for example, for impact phenomena with velocities close to that of the sound velocity, detonation, explosion, cumulation, explosion welding, and transient motions of liquids with free surfaces. Note that because of the accumulation of errors in the boundary conditions, the solution accuracy provided by through calculation Eulerian algorithms is frequently insufficient for acceptable modeling of contact phenomena in materials with clearly pronounced hyperelastic properties that characterize the resistance of the material subjected to long-term, slow, low loading. In the case of modeling long-term processes, a loss of accuracy can be observed.

Shock capturing algorithms have been developed for through calculations of discontinuous solutions in Eulerian algorithms of hydromechanics. These algorithms can be applied together with Lagrangian marker methods to increase the accuracy of the numerical integration of the transport equation when tracking interfacial boundaries and contact discontinuities. To familiarize oneself with shock capturing methods, one can turn to reviews and outlines presented in many modern publications on the numerical methods for calculation of compressible flows, e.g., [76, 378, 610]. The further refinement of the solution near the interfacial boundaries can be achieved by applying adaptive grids.

Adaptive grid algorithms reduce the approximation errors of grid methods in high-gradient regions by means of local reduction of the grid step, optimization of the cell shape, and adaptation of grids to subdomain boundaries and solutions, in particular, to discontinuities and boundary layers. Such an approach has been suggested by the analysis of grid approximation errors. This analysis shows that these errors are proportional to the norm of the derivatives and a certain power of the characteristic step of the grid and increase in case of the appearance of salient points or distortions in the grid cell shape [558].

The development of the moving adaptive grid method is dealt with in [89, 121, 153, 214, 224, 244, 281, 294, 295, 305, 361, 407, 411, 412, 563, 577]. In these publications, the reader can find more comprehensive analysis and review of investigations related to the method. Characteristic of such algorithms are the preservation of the number of grid nodes during the solution and increase in the accuracy due to an optimal arrangement of the nodes (adaptation).

An approach to the description of contact boundaries based on local refinement and reconstruction of grids (adaptive mesh refinement method) is presented and discussed in [79–81, 102, 214, 415, 573, 589]. In this method, the number of the grid nodes and cells is variable.

10. From mesh-based algorithms to meshless ones

A tendency to avoid complications associated with the construction of grids and to design a more economic and simple technique for the numerical solution has led to two extensive fields in the development

of contact algorithms. One of these fields deals with boundary element (boundary integral equation) methods, and the other with a large family of meshless free point algorithms.

The *boundary element algorithms* have been considered in [6, 7, 78, 144, 171, 190, 226, 227, 367, 368]. The boundary element methods are based on the reduction of the classical linear equations of continuum mechanics to boundary integral equations by representing solutions of these equations as the superposition of fundamental solutions corresponding to unit excitations or by using Green's influence functions. The discretization of these equations does not require a volume grid; it suffices to introduce a grid of boundary elements, which reduces the dimension of problems to be solved by one. In a number of algorithms, the stage of the derivation of the boundary integral equations is omitted and the discretized equations are derived straightforwardly on the basis of the fundamental solutions for unit excitations [61, 141, 494].

In nonlinear problems, the solution is constructed by means of external iterations with respect to nonlinear terms. At each iteration, a linearized problem with the classical linear operator is solved. The right-hand sides of these equations involve the nonlinear terms calculated on the basis of the previous iteration. Difficulties arising in this approach are associated with the necessity to calculate volume integrals on the right-hand sides, which requires a volume grid to be introduced, as well as with catastrophic deterioration of convergence of the external iterations as the influence of nonlinear terms increases.

Free Lagrangian discrete algorithms are an attempt to avoid difficulties associated with the distortions of the cells of moving grids when tracking the interfacial boundaries. To that end, the grid is reconstructed step by step with variable neighborhood of grid nodes [2, 12, 159, 160, 214, 218, 438, 481, 583]. The conservative interpolation of the solution on moving grids with variable topology is a nontrivial operation. An algorithm for this operation has been proposed in [2].

Meshless contact algorithms are the further step to the rejection of grids for free Lagrangian nodes (markers/particles). These algorithms are based on the Galerkin–Petrov method with specific basis functions. These functions are not compactly supported but decay rapidly. The basis functions are constructed with the arrangement of the Lagrangian nodes (particles) being taken into account. (The unification of the nodes into cells is not required.) The development of these algorithms can be traced by [71, 72, 125, 127, 168, 215, 408, 413, 414, 429, 438, 458, 459].

In the first studies, Gaussian numerical integration procedures were utilized to derive the system of equations for the discrete problem. This caused certain computational difficulties. Improved numerical integration algorithms (stabilized conforming nodal integration (SCNI) algorithms) are presented in [127]. A simplification of the derivation of equations for the discrete problem is based on the collocation method, which corresponds to the utilization of projection basis of delta-functions.

At the present time, meshless methods have started successfully competing with the traditional grid methods when utilized for the numerical modeling of contact in the case of large deformation and complex rheology [255, 319, 630] and in the case of complex fluid-structure interactions [458, 459].

11. Taking into account contact friction.

In many technological problems, taking into account contact friction plays a decisive role. This is the case, for example, for the modeling of the operation of automotive brakes. For reviews of numerical-analytical methods to taking into account friction, see [5, 84, 205, 234, 237] and the book of reviews [587].

Consider typical models of contact friction that are utilized in discrete numerical algorithms. Note first the modification of Coulomb's friction classical model [433], in which friction forces are constrained by limiting values of the tangential stresses sustained by the contacting media. In accordance with this model, the contact shear stress is constrained by the lower of the yield stresses of the contacting materials. This concept has been developed in detail in [601]. In accordance with the model of [601], the tangential jump of the displacement is divided into the microdisplacement, due to contact elastic strain, and the macrodisplacement, due to plastic (irreversible) smooth of the roughness.

A second example of the friction law which is frequently utilized is the dynamic (viscous) friction model, in which friction contact loads depend on the jump in the tangential velocity [452]. A detailed analysis of friction laws for calculating large strains is given in [130].

For the description and review of contact algorithms that take into account friction see [14, 15, 41, 75, 76, 91, 93, 95, 107, 116, 123, 124, 128, 134, 199, 251, 304, 317, 328, 331, 338, 364–366, 369, 383, 386, 387, 395, 401–403, 409, 560, 566, 623, 626].

Publications [38, 45, 46, 120, 175, 183, 184, 320, 321, 452, 467, 468] are devoted to the modeling of

contact processes with rolling friction. The general Eulerian-Lagrangian approach to rolling is presented in [403].

12. Reviews of problem-oriented contact algorithms.

In this section, we indicate reviews and separate papers that deal with problem-oriented contact algorithms adapted to specific applications.

Animation contact algorithms utilize simple non-iterative explicit methods which do not imply the laws of mechanics to be observed and satisfy the impenetrability constraints by means of heuristic approaches to provide a minimum plausibility for the result. The animation algorithms are aimed at the creation of a cartoon (of dinosaur film type) to visualize contact phenomena. A distinctive feature of the animation algorithms, as compared with continuum mechanics algorithms, is that the former algorithms should allow the animator to change the scenario of motion of the contacting bodies and media when creating the cartoon. As an example of algorithms of that type, one could mention the free shape deformation algorithm [534] and the algorithm for imitating the skin/skeleton deformation [406]. For more detail see the review of [54].

Contact algorithms for applications in medicine and biology. A more proximate approach to reality is necessary in medicine for modeling surgical operations, designing training programs, and predicting the results of plastic surgery. These goals can be achieved by models that partly satisfy the laws of solid mechanics and take into account the strength properties of materials [166, 239, 343].

These simplified models should be replaced by full-scale contact algorithms (developed within the framework of continuum mechanics) as the desired degree of agreement between reality and the model increases. Continuous increase in the productivity of computers favors the intensification of research on the development of algorithms for modeling the motion of living bodies, with the complex internal structure of these bodies being taken into account. However, there have been very few such works so far and they utilize rather simple mechanical models. Mechanical properties of living bodies have been considered in [203]. The animation of contact interactions of elastic bodies for applications in medicine has been attempted in [34, 435, 570, 631]. Reviews of contact algorithms that can be applied in medicine are given in [280, 342].

For a review of contact algorithms for geomechanics see [439], for flows with free moving boundaries [25, 197, 213, 305, 427, 543, 552, 571, 605, 622], for phase change boundaries [299, 567, 581], for thermal effects [540], for cavitation [592], and for modeling of the behavior of cloths [35]. The publications of [536, 538], on the contact tracking on the basis of level set function methods deserve special attention in view of astonishing variety of applications.

13. Contact interaction optimization algorithms.

In the general case, the distribution of the contact loads is nonuniform and depends on the shape of the contact surface. The contact loads can have undesirable peaks which make worse the characteristics of technological processes and reduce the life time of engineering products. One of the first attempts to make the load distribution more uniform by means of optimizing the shape of the contact surface was done in [139]. The optimization was performed on the basis of linear programming. This theme was developed in [271] where the linear programming was utilized in combination with the finite element method. In [56, 132, 135, 475], the optimization was performed on the basis of nonlinear programming. Objective functions for the optimization of contact surfaces were proposed in [179, 180].

A simplified iterative procedure for smoothing peaks of the contact loads for constant volume of the contacting bodies was proposed in [565]. The further simplification was provided by the evolutionary structural optimization (ESO) algorithm. This algorithm was proposed in [606, 607] and can be applied to a wide class of contact optimization problems.

All optimization problems solved in the cited publications have been considered for the cases of rather simple rheology (linear isotropic elasticity) and geometry (2D static problems for two contacting bodies) and have illustrative character. This direction is at the development stage yet [535].

14. Vectorization and parallelizing of contact algorithms.

Discrete models for the analysis of contact interactions in complex structures involve a very large number of nodes. To obtain solutions for such models in a reasonable time, the utilization of vector and multiprocessor computers can be of help. For that reason, many studies related to contact problems have been devoted to vectorization and parallelizing of the available contact algorithms. Issues of the vectorization of contact algorithms were considered in [92, 93, 95, 217, 256, 259, 261].

Parallel computers of various types were tested in the 1980–90s. At the present time, the most suitable

for parallelizing algorithms for solving mathematical physics problems are developed for distributed memory MIMD (Multiple Instruction, Multiple Data) computers, see [453, 512]. Various parallelizing techniques—grid node group decomposition, element group decomposition, and domain decomposition—have been tested. The domain decomposition method (DDM) turned out to be most convenient. For the fundamentals of this method as applied to contact problems, see [114, 185–187, 417, 453].

The fictitious domains formed in accordance with the domain decomposition method have overlapped boundaries on which the solution must be continuous. This continuity is provided by the exchange of the boundary data between the processors during the iterative process. The conjugate gradient method turned out to be one of the most effective and convenient for parallelizing and vectorization. The application of this method to contact problems has been dealt with in [92, 93, 95, 422, 425, 453, 611, 612].

Considered above contact searching algorithms (such as global LPOCA, HITA and local pinball, master–slave, etc.) primarily are not intended for use in parallel computing and their implementation may sufficiently dismiss the profit in performance expected. In parallel codes the contact surface is represented as a set of boundary subdomains, which are processed by using additional processors, which are different from those used for interior subdomains (see, [285, 453]). Parallelized contact algorithms are presented also in [20, 21, 216, 418, 419, 496].

The highest performance of computations achieved for 2001 by means of parallelizing of high-speed impact contact problems was due to a state research organization Sandia National Laboratories (SNL) in the USA. This record has been established by running the parallelized software package PRONTO on the Intel Teraflop Computer (3600 processors). A speed of 1/10 second per time step was achieved for models with the number of 3D 8-node finite elements exceeding 10–15 million. A number of test problems have been solved, from simple tests to an important practically problem of an aircraft crash, with the deformation in the aircraft structure, fuel hydrodynamics (particle method), and the ground deformation being taken into account. The last problem has been hopeless to be solved numerically until recently. In this problem, all contact phenomena that have been discussed previously (including self contact and multiple contact) and through calculation method have occurred. This record computation is presented in the SNL report [22].

Taking into account an intensive development of parallel computers, changes in their architecture and software, and possible expansion into the PC world, one could anticipate the issue of the adaptation of contact algorithms to parallel computers to become rather topical in the nearest time.

On the other hand, one should not overestimate the value of this direction. The point is that the share of parallel computers among the available computer park has been rather small so far and that such computers have been utilized in a remote access mode. This sharply increases the time of waiting for the solution and creates a paradoxical situation. Formally, the time of computation is sharply reduced but in fact for particular user this time may be even increased because of small speed of data transfer through a network and because of possible competition between users, since parallel computers are multiple-user shared computers. As compared with the traditional scalar programming, the parallelizing of codes requires much more effort and cardinal reprogramming and revision of common scalar algorithms. Therefore, to be a success the parallelizing requires high-performance hardware and a powerful financial support, which is feasible only for large research centers working under large-scale state contracts.

When planning work on the parallelizing of contact algorithms, one should also take into account temporal characteristics, specifically, the life time of the parallel computer and its software, the time required for the development of the parallel version of the code, and the time during which the parallel computer can be regarded as a supercomputer. The last remark is due to the fact that scalar computers (including PCs) are also rapidly developing and very often can compete in all aspects with many types of parallel computers that until recently had been acknowledged to be supercomputers. For example, a comparison of a modern PC Pentium/4 with a ten-years-old parallel "8-head" Parsytec will hardly be in favor of the latter.

15. Accuracy analysis and comparison of contact algorithms.

Virtually all contact algorithms provide only approximate solutions. An important aspect of research related to contact algorithms involves the investigation of the accuracy of such algorithms and a priori/a posteriori analysis of errors of the numerical solution. It should be noted that this direction has not been thoroughly developed yet. For the evaluation of the accuracy of Lagrangian algorithms, see, for example, [23, 24, 55, 400, 401, 403, 541, 580, 585, 633]. A review of publications on the evaluation of the accuracy of the Eulerian continuous marker algorithm is given in [115].

Comparative analysis of various approaches is complicated by the fact that the success or failure of a contact algorithms is influenced by the quality of the code and specific features of the algorithms that have not been documented. Unfortunately, there have been only few publications so far in which the same authors compare various approaches. Comparisons that have been performed at the same “kitchen” provide clearer and more definite results. The point is that a minor feature of the algorithm that seems to be unimportant at first sight and has not been mentioned in papers and reports can frequently play a decisive role in the success or failure of the entire algorithm. This is not due to malicious intent of the authors to “keep secret” but most frequently because of a plenty of components of the algorithm and ambiguity of possible formulations of it.

Paper [509] can serve as an example of classic comparative analysis of contact algorithms. In this paper, the quality of numerical modeling of contact discontinuities by means of various through calculation methods is assessed on the basis of the solution of four test transport problems for a specific distributed scalar substance in prescribed steady velocity fields. These fields correspond to simple translation, rigid-body rotation, an isolated vortex, and a complex strain. Four methods have been tested—the most recent version of the marker-and-cell algorithm, the fluid-in-cell method, the level set method, and the shock capturing methods such as TVD and ENO. These methods are arranged from better to worse as they have been listed above. The continuous marker method has been improved in [174] by means of the new Hybrid Particle Level Set (HPLS) method which combines the discrete and continuous Lagrangian marker techniques in a single algorithm.

Among the publications related to critical analysis of contact algorithms there is a very interesting lecture [315] which presents an ironic collection of typical samples of author partialities in self-estimations of merits of developed codes for continuum mechanics: “it will solve your problem without modifications”; “the manual has everything you need to run the code”; “standardized graphics output, compatible with third party post-processors”; “minimal learning curve”; “executable on all machines with no modifications”; “robust and accurate”; “all physics are compatible”; “user friendly”; “there are no more bugs in the code, only undocumented features”; “you can run the code without the manual”; “the technique was first developed here”. It is hardly possible to contest this criticism. The very fact of simultaneous existence of numerous contact algorithms indicates that these algorithms are not perfect. The author assessments of algorithms and results that appear in papers should be considered very carefully.

16. Conclusion.

There are many hundred works on numerical methods of analysis of contact interactions that have been published in the world during the last 3 or 4 decades. We confined our review to publications on contact algorithms. If we had included, in addition, studies on the physics of contact and publications on solving particular problems, the list of bibliography would have consisted of several thousand items and the length of the review would have exceeded all reasonable limits.

This review can be used as a guide in contact algorithms. It should facilitate the choice of an appropriate algorithm and help one to assess the novelty of newly designed algorithms and to select publications for more detailed study and citing.

Although a great number of contact algorithms have been designed, the basis concepts of these algorithms can be comprehended and classified. One possible classification has been presented in the given review. This classification is not optimal but has been suggested by the material to be sorted.

Acknowledgments

This review was carried out within the framework of the Programs of the Department of Power Engineering, Mechanical Engineering, Mechanics, and Control Processes of the Russian Academy of Sciences “Structural mechanics of materials and structural elements. Interaction of nano-, micro-, meso-, and macro-scale phenomena in deformation and fracture” and “Cumulative damage, fracture, and structural changes in materials due to mechanical and thermal loads” and under financial support of the Russian Foundation for Basic Research (Projects Nos. 01-01-00659 and 05-01-245a).

References

1. F. L. Addessio, D. E. Carroll, J. K. Dukowicz, et al., CAVEAT: A computer code for fluid dynamics problems with large distortion and internal slip, Los Alamos National Laboratory, Report UC-32, 1988.
2. A. A. Aganin and V. B. Kuznetsov, "A method of conservative interpolation of integral parameters of cells of arbitrary grids. Dynamics of shells in a flow," in Proceedings of the Seminar of Kazan Institute of Physics and Technology [in Russian], Kazan, Kazan Institute of Physics and Technology, Issue 18, pp. 144–160, 1985.
3. P. Alart, A. Curnier, "A Mixed Formulation for Frictional Contact Problems prone to Newton like Solution Methods," *Comput. Meth. Appl. Mech. Engng.* Vol. 92, pp. 353–375, 1991.
4. B. Alessandrini, G. Delhommeau, "Simulation of three-dimensional unsteady viscous free surface flow around a ship model," *Intern. J. for Num. Meth. in Fluids*, Vol.19, pp. 321–342, 1994.
5. V. V. Alexandrov and S. M. Mkhitarian, Contact Problems for Bodies with Thin Coatings and Interlayers [in Russian], Nauka, Moscow, 1983.
6. M. H. Aliabadi and C. A. Brebbia (Editors), Computational Methods in Contact Mechanics, Computational Mechanics Publications, Elsevier, Boston, N.Y., Southampton, 1993.
7. M. H. Aliabadi, "Boundary element formulations in fracture mechanics," *AMR*, Vol. 50, No. 2, pp. 83–96, 1997.
8. A. A. Amsden and F. H. Harlow, "A simplified MAC technique for incompressible fluid flow calculations," *J. Comput. Phys.*, Vol. 6, p. 322, 1970.
9. B. D. Annin, O. V. Sadovskaya, and V. M. Sadovskii, "Numerical simulation of a skew impact of plates in the elastoplastic formulation," *Fiz. Mezomekhanika*, Vol. 3, No. 4, pp. 23–28, 2000.
10. B. D. Annin, O. V. Sadovskaya, and V. M. Sadovskii, "Numerical simulation of wave formation during explosion welding in the elastoplastic formulation," Proceedings of Intern. Conf. "Synergetics 2000", Komsomolsk-on-Amur, pp. 52–54. 2000.
11. N. N. Anuchina, "On methods for numerical study of compressible fluid flows in the case of large strains," *Chislennye Metody Mekhaniki Sploshnoi Sredy*, Vol. 1, No. 4, pp. 3–84, 1970.
12. N. N. Anuchina, K. I. Babenko, S. K. Godunov, et al., Theoretical Foundation and Construction of Numerical Algorithms for Problems of Mathematical Physics [in Russian], Nauka, Moscow, 1979.
13. T. Aoki, "Multi-dimensional advection of CIP (cubic-interpolated propagation) scheme," *CFD J.*, Vol. 4, p. 279, 1995.
14. F. Armero and E. Petocz, "Formulation and Analysis of Conserving Algorithms for Frictionless Dynamic Contact/Impact Problems," *Comput. Meth. Appl. Mech. Engng.*, Vol. 158, No. 3/4, pp. 269–300, 1998.
15. F. Armero and E. Petocz, "A New Dissipative Time-Stepping Algorithm for Frictional Contact Problems: Formulation and Analysis," *Comput. Meth. Appl. Mech. Engng.*, Vol. 179, No. 1/2, pp. 151–178, 1999.
16. N. Kh. Arutyunyan, A. V. Manzhirov, and V. E. Naumov, Contact Problems of Mechanics of Accreting Bodies [in Russian], Nauka, Moscow, 1991.
17. N. Asano, "A finite element method applicable to elasto-impact contact structures," *Mem. Fac. Eng. Tamagawa Univ.*, No. 17, pp. 39–54, 1982.
18. N. Asano, "A virtual work principle using penalty function method for impact contact problem of two bodies," *Trans. Jap. Soc. Mech. Eng.*, Vol. A51, No. 467, pp. 1863–1898, 1985.
19. V. V. Astanin, Sh. U. Galiev, and K. V. Ivashchenko, "Specific features of deformation and fracture of aluminum obstacles impacted by a steel projectile along the normal," *Problemy Prochnosti*, No. 12, pp. 52–58, 1988.
20. S. Attaway, T. Barragy, K. Brown, et al., Transient Solid Dynamics Simulations on the Sandia/Intel Teraflop Computer, Gordon Bell finalist paper, Proc. of SuperComputing '97. San Jose, CA, November 1997.

- Internet: <http://www.cs.sandia.gov/~sjplimp/main.html>
21. S. W. Attaway, B. A. Hendrickson, S. J. Plimpton, et al., "A Parallel Contact Detection Algorithm for Transient Solid Dynamics Simulations Using PRONTO3D," *J. Comput. Mech.*, Vol. 22, No. 2, pp. 143–159, 1998.
 22. S. W. Attaway, E. J. Barragy, K. H. Brown, et al., *Transient Solid Dynamics Simulations on the Sandia/Intel Teraflop Computer // Sandia National Laboratories, Albuquerque, 2001, Report NM 87185-0437, 2001.*
Internet: <http://www.cs.sandia.gov/~sjplimp/main.html>
 23. I. Babushka and W. Rheinboldt, "Error estimates for Adaptive Finite Element Computations," *J. Numer. Analysis*, Vol. 15, pp. 736–754, 1978.
 24. I. Babushka and A. Miller, "A feedback finite element method with a posteriori error estimation: Part 1. The finite element method and some basic properties of the a posteriori error estimation," *Comput. Meth. Appl. Mech. Engng.*, Vol. 61, pp. 1–40, 1987.
 25. T. A. Baer, R. A. Cairncross, P. R. Schunk, et al., "A finite element method for free surface flows of incompressible fluids in three dimensions. Part II. Dynamic wetting lines," *Intern. J. Numer. Meth. Fluids*, Vol. 33, pp. 405–427, 2000.
 26. L. Baillet, H. Walter, M. Brunet, "A 3D contact algorithm using an explicit FEM applied to ironing process," *Proc. 4th Intern. Conf. and Workshop on Numer. Simulation of 3D Sheet Forming Processes (NUMISHEET 99) / Eds. J.-C. Gelin et P. Picart. Besanson, France*, pp. 209–214, 1999.
 27. M. Baker, P. Cocs, P. Wastein, et al., *Explosion Phenomena, Estimates and Implications [Russian translations]*, in 2 volumes, Mir, Moscow, 1986.
 28. S. M. Bakhrakh, Yu. P. Glagoleva, M. S. Samigulin, V. D. Frolov, and Yu. V. Yanilkin, "Modeling of gas dynamic flow on the basis of the concentration method," *Doklady AN SSSR*, Vol. 257, No. 3, pp. 566–569, 1981.
 29. S. M. Bakhrakh, V. F. Spiridonov, and A. A. Shanin, "A method for computation of 2D axially symmetric gas dynamic flows of a heterogeneous medium in terms of Lagrangian-Eulerian variables," *Doklady AN SSSR*, Vol. 276, No. 4, pp. 829–833, 1984.
 30. S. Bakhrakh, M. Samigulin, V. Sevastianov, Yu. Yanilkin, "The EGAK Method for Calculating Gas Flows of Heterogeneous Media in Eulerian Coordinates," in *Numerical Methods in Fluid Dynamics*, MIR, Moscow, 1984.
 31. N. V. Banichuk, "Numerical solution of the problem of bending of a constrained elastic plate," *Inzhenernyi Zhurnal MTT*, No. 4, pp. 138–142, 1967.
 32. N. V. Banichuk, V. M. Kartvelishvili, and F. L. Chernous'ko, "Numerical solution of the problem of indentation of a punch into an elastoplastic medium," *Izv. AN SSSR. MTT [Mechanics of Solids]*, No. 1, pp. 50–57, 1972.
 33. N. V. Banichuk and F. L. Chernous'ko, *Variational Problems of Mechanics and Control [in Russian]*, Nauka, Moscow, 1973.
 34. D. Baraff and A. Witkin, "Dynamic simulation of non-penetrating flexible bodies," *Proc. SIGGRAPH 92, Computer Graphics*, Vol. 26, No. 2, pp. 303–308, 1992.
 35. D. Baraff and A. Witkin, "Large steps in cloth simulation," *Proc. SIGGRAPH 98, Computer Graphics Proceedings, Annual Conf. Series*, pp. 43–54, 1998.
 36. F. J. Bartold and D. Bischoff, "Generalization of Newton type Methods to Contact Problems with Friction," *J. Mech. Theor. Appl.*, Special issue: *Numerical Methods in Mechanics of Contact Involving Friction*, pp. 97–110, 1988.
 37. V. V. Bashurov, Yu. A. Bondarenko, E. V. Gubkov, et al., *Experimental and Numerical Study of the Development of Deterministic 2D Perturbation of a Contact Boundary Accelerated by a Series of Shock Waves [in Russian]*, Preprint No. 45–96, VNIIEF, 1996.
 38. J. M. Bass, "Three dimensional finite deformations rolling contact of a hyperelastic cylinder: formulation of the problem and computational results," *Computers and Structures*, Vol. 26, No. 6, pp. 991–1004, 1987.

39. K. J. Bathe and A. Chaudhary, "A solution method for planar and axisymmetric contact problems," *Intern. J. Numer. Meth. Engng.*, Vol. 21, pp. 65–88, 1985.
40. K. J. Bathe and A. Chaudhary, "A solution method for static and dynamic analysis of three-dimensional contact problems with friction," *Computers and Structures*, Vol. 24, No. 6, pp. 855–873, 1986.
41. K. J. Bathe and S. S. Mijailovich, "Finite-element analysis of frictional contact problems," *J. Mec. Theor. Appl.*, Vol. 7, pp. 31–45, 1988.
42. K. J. Bathe, H. Zhang, M. H. Wang, "Finite element analysis of incompressible and compressible flows with free surfaces and structural interactions," *Comput. Meth. Appl. Mech. Engng.*, Vol. 56, pp. 193–213, 1995.
43. K. J. Bathe, *Finite Element Procedures*. EngleWood Cliffs: Prentice-Hall, 1996.
44. K. J. Bathe and P. A. Bouzinov, "On the constraint function method for contact problems," *Computers and Structures*, Vol. 64, No. 5–6. pp. 1069–1085, 1997.
45. R. C. Batra, "Rubber covered rolls - the non linear elastic problem," *J. Appl. Mech.*, Vol. 47, No. 1, pp. 82–86, 1980.
46. R. C. Batra, "Quasistatic indentation of a rubber-covered roll by a rigid roll," *Intern. J. Numer. Meth. in Engng*, Vol. 17, No. 12, pp. 1823–1833, 1981.
47. V. G. Bazhenov, S. V. Zefirov, and M. V. Petrov, "Numerical solution of problems of transient contact interaction of elastoplastic shells of revolution in the case of large deformations," in *Algorithmization and Automation of Solving Problems of Elasticity and Plasticity* [in Russian], Izd-vo Gorkovskogo Universiteta, Gorky, Issue 28, pp. 54–59, 1984.
48. V. G. Bazhenov, A. G. Kibets, and A. I. Sadyrin, "A modification of the Wilkins algorithm for numerical solution of 3D dynamic problems," in *Applied Problems of Strength and Plasticity. Algorithms and Software for Strength Problems* [in Russian], Izd-vo Gorkovskogo Universiteta, Gorky, Issue 34, pp. 14–19, 1986.
49. V. G. Bazhenov and A. G. Kibets, "Numerical finite-element models of transient deformation of elastoplastic structures," *Izv. RAN. MTT [Mechanics of Solids]*, No. 1, pp. 52–57, 1994.
50. V. G. Bazhenov, A. G. Kibets, and I. N. Tsvetkova, "Numerical simulation of impact interaction transient processes in deformable structural members," *Problemy Mashinostroeniya i Nadezhnosti Mashin*, No. 2, pp. 20–26, 1995.
51. V. G. Bazhenov, A. G. Kibets, and I. N. Tsvetkova, "Finite-element models of transient processes of contact interaction of composite structure components in 3D dynamic problems," in *All-Russia Symposium "Dynamic and Technological Problems in Structural and Continuum Mechanics"*. Abstracts of Papers [in Russian], MAI, Moscow, p. 8, 1995.
52. V. G. Bazhenov, A. G. Kibets, and I. N. Tsvetkova, "Numerical simulation of transient contact interaction of deformable structures," in *Applied Problems of Strength and Plasticity. Numerical Simulation of Processes in Physics and Mechanics* [in Russian], Tovarishchestvo Nauchnykh Izdaniy KMK, Moscow, Issue 52, pp. 154–160, 1995.
53. M. Beddhu, M. Y. Jiang, K. Lafayette, et al., "Computation of steady and unsteady flows with a free surface around the Wigley hull," *Appl. Mathematics and Computation*, Vol. 89, pp. 67–84, 1998.
54. D. Bechmann, "Space deformation models survey," *Computer Graphics*, Vol. 18, No. 4, pp. 571–586, 1994.
55. R. Becker and R. Rannacher, "A Feed-Back Approach to Error Control in Finite Element Methods: Basic Analysis and Examples," *EAST-WEST J. Numer. Math.*, Vol. 4, pp. 237–264, 1996.
56. A. D. Belegundu and T. R. Chandrupatla, "Shape Optimization of Valve Geometry with Contact Analysis," *Sensitivity Analysis and Optimization with Numerical Methods* / Eds. S. Saigal, S. J. Mukherjee, pp. 71–78, 1990.
57. V. Belikov and A. Semenov, Non-Sibsonian interpolation on arbitrary system of points in Euclidean space and adaptive generating isolines algorithm. *Numerical Grid Generation in Computational Field Simulation*, Proc. of the 6th Intl. Conf. Greenwich Univ. July 1998.

58. O. M. Belotserkovskii (editor), Numerical Methods in Fluid Mechanics [in Russian], Mir, Moscow, 1973.
59. O. M. Belotserkovskii and Yu. M. Davydov, Large Particle Method in Gas Dynamics [in Russian], Nauka, Moscow, 1982.
60. O. M. Belotserkovskii, Numerical Methods in Continuum Mechanics [in Russian], Nauka, Moscow, 1984.
61. S. M. Belotserkovskii and M. I. Nisht, Separated and Unseparated Flow of an Ideal Fluid around Thin Airfoils [in Russian], Nauka, Moscow, 1978.
62. N. N. Belov, V. N. Demidov, L. V. Efremova, et al., "Computer simulation of high-speed impact dynamics and related physical phenomena," *Izv. Vuzov. Fizika*, No. 8, pp. 5–48, 1992.
63. T. Belytschko, D. P. Flanagan, and J. M. Kennedy, "Finite element methods with user-controlled meshes for fluid-structure interaction," *Comput. Methods Appl. Mech. Engng*, Vol. 33, p. 669, 1982.
64. T. Belytschko, J. M. Kennedy, J. I. Lin, "Three-dimensional penetration computation," *Trans. 9th Intern. Conf. Struct. Mech. React. Technol.*, Lausanne, pp. 83–88, 1987.
65. T. Belytschko, J. I. Lin "A three dimensional impact-penetration algorithm with erosion," *Computers and Structures*, Vol. 25, No. 3, pp. 95–104, 1987.
66. T. Belytschko and J. I. Lin, "A three dimensional impact-penetration algorithm with erosion," *Intern. J. Impact Engng.*, Vol. 5, No. 1–4, pp. 111–127, 1987.
67. T. Belytschko, B. L. Wong, E. J. Plaskacz, "Fission-fusion adaptivity in finite elements for nonlinear dynamics of shells," *Computers and Structures*, Vol. 33, No. 5, pp. 1307–1323, 1989.
68. T. Belytschko and M. O. Neal, "Contact-Impact by the Pinball Algorithm with Penalty Projection and Lagrangian Methods," *Proc. Symp. on Comput. Techniques for Impact. Penetration and Perforation of Solids.* / Eds. L.E. Schwer et al. ASME. Winter Annual Meeting. San Francisco, CA, AMD, Vol. 103, 1989.
69. T. Belytschko and M. O. Neal, "Contact-Impact by the Pinball Algorithm with Penalty and Lagrangian Methods," *Intern. J. Numer. Methods in Engng.*, Vol. 31, No. 3, pp. 547–572, 1991.
70. T. Belytschko and L. S. Yeh, "The splitting pinball method for contact-impact problems," *Comput. Meth. Appl. Mech. Engng.*, Vol. 105, No. 3, pp. 375–393, 1993.
71. T. Belytschko, Y. Y. Lu, L. Gu, "Element-Free Galerkin Methods," *Intern. J. Numer. Meth. Engng.*, Vol. 37, No. 2, pp. 229–256, 1994.
72. T. Belytschko, Y. Kronggauz, D. Organ, et al., "Meshless Methods: An Overview and Recent Developments," *Comput. Meth. Appl. Mech. Engng.*, Vol. 139, No. 1–4, pp. 3–47, 1996.
73. H. Benaroya, "Localization and effects of irregularities in structures," *AMR*, Vol. 49, No. 2, pp. 55–135, 1996.
74. D. J. Benson and J. O. Hallquist, "A single surface contact algorithm for the postbuckling analysis of shell structures," Report BN, San Diego: Univ. of California, 1987.
75. D. J. Benson and J. O. Hallquist, "A single surface contact algorithm for the postbuckling analysis of shell structures," *Comput. Meth. Appl. Mech. Engng.*, Vol. 78, No. 2, pp. 141–163, 1990.
76. D. J. Benson, "Computational methods in Lagrangian and Eulerian hydrocodes," *Comput. Meth. Appl. Mech. Engng.*, Vol. 99, No. 2–3, pp. 235–394, 1992.
77. D. J. Benson, "Volume of fluid interface reconstruction methods for multi-material problems," *AMR*, Vol. 55, No. 2, pp. 151–165, 2002.
78. P. Berenji and R. Butterfield, *Boundary Elements in Applied Sciences* [Russian translation], Mir, Moscow, 1984.
79. M. J. Berger and J. Olinger "Adaptive mesh refinement for hyperbolic partial differential equations," *J. Comp. Phys.*, Vol. 53, No. 3, pp. 481–512, 1984.
80. M. J. Berger and A. Jameson, "Automatic adaptive grid refinement for the Euler equations," *AIAA J.*, Vol. 23, No. 561, pp. 3–6, 1985.
81. M. J. Berger, P. Colella, "Local adaptive mesh refinement for shock hydrodynamics," *J. Comp. Phys.*, Vol. 82, No. 1, pp. 64–84, 1989.

82. L. D. Bertholf, L. D. Buxton, B. J. Thorue, et al., "Damage in steel plates from hypervelocity impact II. Numerical results and spall measurement," *J. Appl. Phys.*, Vol. 46, No. 9, pp. 3776–3783, 1975.
83. D. P. Bertsekas, *Constraint Optimization and Lagrange Multiplier Methods*. N.Y., Academic Press, 1984.
84. B. Bhushan, "Contact mechanics of rough surfaces in tribology: Single asperity contact," *AMR*, Vol. 49, No. 5, pp. 275–298, 1996.
85. G. Bjorkman, A. Klarkbring, A. Sjodin, et al., "Quadratic Programming for Non-Linear Elastic Contact Problems," *Intern. J. Numer. Meth. Engng.*, Vol. 38, pp. 137–165, 1995.
106. G. Brode, *Computer Simulation of Explosion [Russian translation]*, Mir, Moscow, 1976.
87. R. de Borst, "Smearred cracking, plasticity, creep and thermal loading - a unified approach," *Comp. Meth. Appl. Mech. Engng.*, Vol. 62, pp. 89–110, 1987.
88. R. de Borst, "Fracture in quasi-brittle materials: a review of continuum damage-based approaches," *Engng. Fracture Mech.*, Vol. 69, pp. 95–112, 2002.
89. N. G. Bourago, "Formulation of equations of continuum mechanics in moving adaptive coordinates," in *Numerical Methods in Solid Mechanics [in Russian]*, Computing Center AN SSSR, Moscow, pp. 32–49, 1984.
Internet: <http://www.ipmnet.ru/burago/papers/grid.htm>
90. N. G. Bourago, "A method for numerical simulation of impact contact interaction of elastoplastic bodies," *Materials of the 6th All-Union Congress on Theoretical and Applied Mechanics [in Russian]*, Tashkent, pp. 142–143, 1986.
91. N. G. Bourago, "Finite-element computational models of contact interaction of elastoplastic bodies in the case of an impact with transonic velocities," in *Theory of Propagation of Waves in Elastic and Elastoplastic Media. 8th All-Union Symposium [in Russian]*, Institut Gornogo Dela SO AN SSSR, Novosibirsk, pp. 74–79, 1987.
92. N. G. Bourago, "On the vectorization of the finite-element method on unstructured grids for solving problems of elasticity and plasticity," in *Numerical Formulation of Physical and Mechanical Problems of Strength. 2nd All-Union Conference [in Russian]*, Gorky, pp. 53–54, 1987.
93. N. G. Bourago and V. N. Kukudzhakov, *Solution of Elastoplastic Problems by the Finite Element Method. Code ASTRA [in Russian]*, Preprint No. 326, Institute for Problems in Mechanics of RAS, Moscow, 1988.
94. N. G. Bourago, "Numerical simulation of the explosion of a charge of an arbitrary shape in a geomaterial," in *Proc. All-Union Conf. "Deformation and Fracture of Rocks" [in Russian]*, ILIM, Frunze, pp. 49–56, 1990.
95. N. G. Bourago and V. N. Kukudzhakov, "Solution of problems of elastoplasticity by the Finite Element Method," in *Computational Mechanics of Solids [in Russian]*, Nauka, Moscow, Issue 2, pp. 78–122, 1991.
Internet: <http://www.ipmnet.ru/burago/papers/rep1988.htm>
96. N. G. Bourago, A. I. Glushko, and A. N. Kovshov, "Thermodynamic method for the derivation of constitutive relations for models of continuous media," *Izv. RAN. MTT [Mechanics of Solids]*, No. 6, pp. 4–15, 2000.
97. N. G. Bourago and V. N. Kukudzhakov, "On the damage and strain localization," in *Applied Problems of Strength and Plasticity [in Russian]*, Izd-vo Nizhegorodskogo Universiteta, Nizhny Novgorod, Issue 63, pp. 41–48, 2001.
98. N. G. Bourago, V. I. Kondaurov, and V. N. Kukudzhakov, "Numerical simulation of damage of elastoplastic bodies," in *Scientific Session MIFI-2002, Science-and-Technology Conference "Science-and-innovation Cooperation". Collected Proceedings [in Russian]*, MIFI, Moscow, Part 1, pp. 95–96, 2002.
99. N. G. Bourago, "A Survey on Contact Algorithms," *Proc. Intern. Workshop on Grid Generation and Industrial Applications. Moscow: Computing Centre of RAS*, pp. 42–59, 2002.

100. N. G. Bourago and V. N. Kukudzhanov, Numerical Solution of Damage Problems [in Russian], Preprint No. 746, Institute for Problems in Mechanics, Moscow, 2004.
Internet: <http://www.ipmnet.ru/burago/papers/prepr03.htm>
101. F. P. Bowden and D. Tabor, *The Friction and Lubrication of Solids. Part II.* Oxford: Clarendon press, 1964.
102. J. U. Brackbill and J. S. Saltzman, "Adaptive zoning for singular problems in two dimensions," *J. Comput. Phys.*, Vol. 46, No. 3, pp. 342–368, 1982.
103. J. U. Brackbill, D. B. Kothe, H. M. Ruppel, "FLIP: A low dissipation, particle-in-cell method for fluid flow," *Comput. Phys. Commun.*, Vol. 48, No. 1, pp. 25–38, 1988.
104. J. U. Brackbill, D. B. Kothe, C. Zemach, "A continuum method for modeling surface tension," *J. Comput. Phys.*, Vol. 100, p. 335, 1992.
105. K. Brown, S. Attaway, S. Plimpton, et al., "Parallel strategies for crash and impact simulations," *Comput. Meth. Appl. Mech. Engng.*, Vol. 184, No. 2–4, pp. 375–390, 2000.
106. G. Brode, *Computer Simulation of Explosion* [Russian translation], Mir, Moscow, 1976.
107. M. A. Brunet, "A solution method for large strain of anisotropic material with contact and friction boundary conditions," *Proc. 5th Intern. Symp. Numer. Meth. Engng.*, Lausanne-Switzerland, Berlin: Springer, Vol. 2, pp. 369–374, 1989.
108. A. N. Bugrov, A. N. Kononov, and V. A. Shcherbak, "Fictitious domain methods in plane static problems of elasticity," *Chislennyye Metody v Mekhanike Splushnoi Sredy*, Vol. 5, No. 1, pp. 20–30, 1974.
109. A. M. Bykovskikh, V. D. Koshur, V. A. Mart'yanov, and I. V. Filimonenko, "Modeling of dynamic processes of impact and penetration," in *Numerical Methods for Solving Problems of Elasticity and Plasticity. Proc. 13th Inter-republican Conference* [in Russian], ITPM SO RAN, Novosibirsk, pp. 30–35, 1995.
110. O. V. Bychek and V. M. Sadovskii, "Investigation of dynamic contact interaction of solids," *PMTF*, Vol. 39, No. 4, pp. 167–173, 1998.
111. L. T. Campos, J. T. Oden, N. Kikuchi "A Numerical Analysis of a Class of Contact Problems with Friction in Elastostatics," *Comput. Meth. Appl. Mech. Engng.*, Vol. 34, No. 1–3, pp. 821–845, 1982.
112. G. Carey, *Computational grids: Generation, Adaptation and Solution Strategy.* Florida: Taylor and Francis, 1997.
113. N. J. Carpenter, R. L. Taylor, M. G. Katona, "Lagrange constraints for transient finite-element surface-contact," *Intern. J. Num. Meth. Engng.*, Vol. 32, pp. 103–128, 1991.
114. W. T. Carter Jr, T.-L. Sham, K. H. Law, "A parallel finite element method and its prototype analysis of shell structures," *Computers and Structures*, Vol. 31, No. 1, pp. 921–934, 1989.
115. G. Cerne, S. Petelin, I. Tiselj, "Numerical errors of the volume-of- fluid interface tracking algorithm," *Intern. J. Numer. Meth. Fluids*, Vol. 38, No. 1, pp. 329–350, 2002.
116. S. Cescotto and R. Charlier, "Frictional Contact Finite Elements Based on Mixed Variational Principles," *Intern. J. Numer. Meth. Engng.*, Vol. 36, No. 10, pp. 1681–1701, 1993.
117. S. Cescotto and Y. Y. Zhu, "Large Strain Dynamic Analysis using Solid and Contact Finite Element Based on a Mixed Formulation; Application to Metal Forming," *J. of Mater. Proces. Techn.*, Vol. 45, No. 1–4, pp. 657–663, 1994.
118. S. H. Chan and I. S. Tuba, "A Finite Element Method for Contact Problems in Solid Bodies," *Intern. J. Mech. Sci.*, Vol. 13, pp. 615–639, 1971.
119. N. Chandrasekaran, W. E. Haisler, R. E. Goforth, "A finite element solution method for contact problems with friction," *Intern. J. Numer. Meth. Engng.*, Vol. 24, pp. 477–495, 1987.
120. J. P. Chang, K. Satyamurthi, N. T. Tseng, "An efficient approach to the three-dimensional finite element analysis of tires," *Tire Sci. Technol.*, Vol. 16, No. 4, pp. 249–273, 1988.

121. A. A. Charakhch'yan "A barrier-type grid generator for problems with moving boundaries," in Construction of Numerical Grids: Theory and Applications [in Russian], S. A. Ivanenko and V. A. Garanzha (eds.), Computing Center of the Russian Academy of Sciences, Moscow, pp. 195–206, 2002.
122. P. Charbrand, F. Dubois, M. Raous, "Various numerical methods for solving unilateral contact problems with friction," *Math. Comput. Modelling*, Vol. 28, No. 4–8, pp. 97–108, 1998.
123. A. B. Chaudhary and K. J. Bathe, "A Solution Method for Static and Dynamic Analysis of Three-Dimensional Contact Problems with Friction," *Computer and Structures*, Vol. 24, No. 6, pp. 855–873, 1986.
124. V. Chawla and T. A. Laursen "Energy Consistent Algorithms for Frictional Contact Problems," *Intern. J. Numer. Meth. Engng.*, Vol. 42, No. 5, pp. 799–827, 1998.
125. J. S. Chen, C. Pan, C. T. Wu, et al., "Reproducing Kernel Particle Methods for Large Deformation Analysis of Nonlinear Structures," *Comput. Meth. Appl. Mech. Engng.*, Vol. 139, No. 1–4, pp. 195–229, 1996.
126. J. S. Chen, C. Pan, C. T. Wu, "Large deformation analysis of rubber based on a reproducing kernel particle method," *Comput. Meth. Appl. Mech. Engng.*, Vol. 19, No. 3, pp. 211–227, 1997.
127. J. S. Chen, C. T. Wu, S. Yoon, Y. You, "Stabilized Conforming Nodal Integration for Galerkin Meshfree Methods," *Intern. J. Numer. Meth. Engng.*, Vol. 50, No. 2, pp. 435–466, 2001.
128. W. H. Chen and P. Tsai, "Finite Element Analysis of Elastodynamic Sliding Contact Problems with Friction," *Computers and Structures*, Vol. 22, No. 6, pp. 925–938, 1986.
129. Y. M. Chen and M. L. Wilkins, "Stress Analysis of Crack Problems a Three-Dimensional Time-Dependent Computer Program," *Intern. J. Fracture*, Vol. 12, No. 4, pp. 607–617, 1976.
130. J. H. Cheng and N. Kikuchi, "An Incremental Constitutive Relation of Unilateral Contact Friction for Large Deformation Analysis," *J. Appl. Mech.*, *Trans. ASME*, Vol. 52, No. 3, pp. 639–648, 1985.
131. T. Y. Cheng, A. F. Saleeb, S. C. Shyu, "Finite Element Solutions of Two-Dimensional Contact Problems Based on a Consistent Mixed Formulation," *Computers and Structures*, Vol. 27, No. 4, pp. 455–466, 1987.
132. W. Q. Cheng, F. W. Zhu, J. W. Luo, "Computational Finite Element Analysis and Optimal Design for Multibody Contact System," *Comput. Meth. Appl. Mech. Engng.*, Vol. 71, No. 1, pp. 31–39, 1988.
133. I. H. Choi and C. S. Hong, "New Approach for Simple Prediction of Impact Force History on Composite Laminates," *AIAA J.*, Vol. 32, No. 10, pp. 2067–2072, 1994.
134. P. W. Christiansen, A. Klarbring, J. S. Pang, N. Stromberg, "Formulation and comparison of algorithms for frictional contact problems," *Intern. J. Numer. Meth. Engng.*, Vol. 42, No. 1, pp. 145–173, 1998.
135. F. H. Clarke, *Optimization and Nonsmooth Analysis*, Wiley, New York, 1983.
136. M. Cocu, "Existence of solutions of Signorini problems with friction," *Intern. J. Engng. Sci.*, Vol. 22, No. 5, pp. 567–575, 1984.
137. M. Cocu, E. Pratt, M. Raous, "Formulation and approximation of quasistatic frictional contact," *Intern. J. Engng. Sci.*, Vol. 34, pp. 783–798, 1996.
138. M. Cocu, E. Pratt, M. Raous, "Constructive aspects of functional analysis for the treatment of frictional contact," *Math. Comput. Modelling*, Vol. 28, pp. 109–120, 1998.
139. T. F. Conry and A. Seireg, "A Mathematical Programming Method for Design of Elastic Bodies in Contact," *Trans. ASME., J. Appl. Mech.*, Vol. 38, No. 2, pp. 387–392, 1971.
140. M. G. Cooper, B. B. Mikic, M. M. Yovanovich, "Thermal Contact Conductance," *Intern. J. Heat Mass Transfer*, Vol. 12, pp. 279–300, 1969.
141. G. H. Cottet and P. Koumoutsakos, *Vortex Methods: Theory and Practice*, Cambridge University Press, 2000.
142. M. A. Crisfield, *Non-linear Finite Element Analysis of Solids and Structures*. N.Y.:Wiley. V. 1. Essentials, 1991; V. 2. Advanced Topics. 1997.
143. W. Crawly "Free Lagrangian Algorithm (FLAG) for numerical simulation of 2D hydrodynamic flows," in *Numerical Methods in Fluid Mechanics [Russian translations]*, Mir, Moscow, pp. 135–145, 1973.

144. T. A. Cruse, *Boundary Element Analysis in Computational Fracture*. Kluwer, Dordrecht, 1988.
145. A. Curnier, "Theory of Friction," *Intern. J. Solids Structures*, Vol. 20, pp. 637–647, 1984.
146. A. Curnier and P. Alart, "A Generalized Newton Method for Contact Problems with Friction," *J. Mec. Theor. Appl.*, Special Issue: Numerical Methods in Mechanics of Contact Involving Friction, pp. 67–82, 1988.
147. A. Curnier, Q. C. He, J. J. Telega, "Formulation of Unilateral Contact between two Elastic Bodies undergoing Finite Deformation," *C. R. Acad. Sci. Paris.*, Vol. 314, pp. 1–6, 1992.
148. A. Curnier, Q. C. He, A. Klarbring, "Continuum Mechanics Modelling of Large Deformation Contact with Friction," *Contact Mechanics / Eds. M. Raous, M. Jean, J. J. Moreau*, N.Y.: Plenum, 1995.
149. C. Daux, N. Moes, J. Dolbow, N. Sukumar, T. Belytschko, "Arbitrary Branched and Intersecting Cracks with the Extended Finite Element Method," *Intern. J. Numer. Meth. Engng.*, Vol. 48, No. 12, pp. 1741–1760, 2000.
150. V. S. Davydov and E. N. Chumachenko, "A method for finite-element modeling of contact interaction for solving problems of shape changes in continuous media," *Izv. RAN. MTT [Mechanics of Solids]*, No. 4, pp. 53–63, 2000.
151. Yu. M. Davydov, "Numerical analysis of Taylor instability in a nonlinear approximation," *Chislennye Metody Mekhaniki Sploshnoi Sredy*, Vol. 9, No. 3, pp. 67–79, 1978.
152. Yu. M. Davydov and M. S. Pantelev, "The development of 3D perturbations in the case of Rayleigh–Taylor instability," *PMTF*, No. 1, pp. 117–122, 1981.
153. N. T. Danaev, V. D. Liseikin, and N. N. Yanenko, "On the movable coordinate method in gas dynamics," in *Problems of Mathematical Physics and Computational Mathematics [in Russian]*, Nauka, Moscow, pp. 107–115, 1977.
154. N. S. Darova, O. A. Dibirov, G. V. Zharova et al., "Code EGAK. Eulerian-Lagrangian method of calculation of 2D gasdynamic flows of multicomponent media," [in Russian], *VANT, Ser. MMFP*, Issue 2, pp. 51–58, 1994.
155. S. Desai, M. M. Zaman, J. G. Lightner, H. J. Siriwardane, "Thin-Layer Element for Interfaces and Joints," *Intern. J. Numer. and Analyt. in Geomech.*, Vol. 8, No. 1, pp. 19–43, 1984.
156. G. Devaut and J. L. Lions, *Inequalities in Mechanics and Physics*, Berlin: Springer, 1976.
157. R. Diekmann, J. Hungershofer, M. Lux, et al., "Using Space Filling Curves for Efficient Contact Searching," 16th IMACS World Congress, 6 p., 2000.
158. G. Dilintas, P. Laurent-Gengoux, D. Trystam, "A conjugate projected gradient method with preconditioning for unilateral problems," *Computers and Structures*, Vol. 29, No. 4, pp. 675–680, 1988.
159. V. F. D'yachenko, "On a new method for numerical solution of gas dynamics unsteady problems with two spatial variables," *Zhurnal Vychislitel'noi Matematiki i Matematicheskoi Fiziki [Journal of Computational Mathematics and Mathematical Physics]*, Vol. 5, No. 4, pp. 680–688, 1965.
160. V. F. Djachenko, "The Free Point Method for Problems of Continuous Media," *Comput. Meth. Appl. Mech. Engng.*, Vol. 2, 1973.
161. J. Dolbow, "An Extended Finite Element Method with Discontinuous Enrichment for Applied Mechanics," PhD thesis, Northwestern University, USA, 1999.
162. J. Dolbow, N. Moes, T. Belytschko, "Discontinuous Enrichment in Finite Elements with a Partition of Unity Method," *Finite Elements Anal., Des.*, Vol. 36, No. 3-4, pp. 235–260, 2000.
163. J. Dolbow, N. Moes, T. Belytschko, "An Extended Finite Element Method for Modeling Crack Growth with Frictional Contact," *Comput. Methods Appl. Mech. Engng.*, Vol. 190, pp. 6825–6846, 2001.
164. I. S. Doltsinis, "Aspects of Modelling and Computation in the Analysis of Metal Forming," *Engng. Computations*, Vol. 7. pp. 2–20, 1990.
165. J. Donea, S. Giuliani, and J. P. Halleux, "An arbitrary Lagrangian-Eulerian finite element method for transient dynamic fluid-structure interactions," *Comput. Methods Appl. Mech. Engng.*, Vol. 33, p. 689, 1982.

166. P. S. Donzelli, "A Mixed-Penalty Contact Finite Element formulation for biphasic soft tissues," PhD Thesis. Dept. of Mech. Eng. Aeronautical Eng. and Mechanics, RPI, Troy, NY, 1995.
167. D. Dowson, *History of Tribology*, N.Y.: Longman, 1979.
168. C. A. Duarte and J. T. Oden, "An h-p Adaptive Method Using Clouds," *Comput. Meth. Appl. Mech. Engng.*, Vol. 139, No. 1-4, pp. 237-262, 1996.
169. C. A. Duarte, O. N. Hamzeh, T. J. Liszka, W. W. Twordzydlo, "A Generalized Finite Element Method for the Simulation of Three-Dimensional Dynamic Crack Propagation," *Comput. Methods Appl. Mech. Engng.*, Vol. 190, No. 15-17, pp. 2227-2262, 2001.
170. J. Duvaut and J.-L. Lions, *Inequalities in Mechanics and Physics* [Russian translation], Nauka, Moscow, 1980.
171. C. Eck, O. Steinbach, W. L. Wendland, "A Symmetric Boundary Element Method for Contact Problem with Friction," *Mathematics and Computers in Simulation*, Vol. 50, No. 1-4, pp. 43-62, 1999.
172. C. Eck and W. L. Wendland, "An Adaptive Boundary Element Method for Contact Problems," *Mathematical Aspects of Boundary Element Method / Eds. M. Bonnet et al.*, pp. 116-127, 1998.
173. B. Elsner, H. G. Galbas, B. Gorg, O. Kolp, G. Lonsdale, "A Parallel Multilevel Contact Search Algorithm in Crashworthiness Simulation," *Advances in Computational Structures Technology: Selected Papers from 3rd Int. Conf. on Comput. Structure Technology*. Budapest: Civil Comp Press., pp. 397-402, 1996.
174. D. Enright, R. Fedkiw, J. Ferziger, and I. Mitchell, "A hybrid particle level set method for improved interface capturing," *J. Comput. Phys.*, Vol. 183, pp. 83-116, 2002.
Internet: <http://graphics.stanford.edu/~fedkiw/papers/stanford2001-04.pdf>
175. T. Endo, J. T. Oden, E. B. Becker, T. Miller, "A numerical analysis of contact and limit-point behavior in a class of problems of finite elastic deformations," *Computers and Structures*, Vol. 18, No. 5, pp. 899-910, 1984.
176. L. W. Ehrlich, "A Numerical Method of Solving a Heat Flow Problem with Moving Boundary," *J. Assoc. Comput. Machinery*, Vol. 5, No. 2, pp. 161-176, 1958.
177. A. L. Eterovic and K. J. Bathe, "On the Treatment of Inequality Constraints Arising from Contact Conditions in Finite-Element Analysis," *Computers and Structures*, Vol. 40, No. 2, pp. 203-209, 1991.
178. A. L. Eterovic and K. J. Bathe, "An Interface Interpolation Scheme for Quadratic Convergence in the Finite Element Analysis of Contact Problems," *Computational Methods in Nonlinear Mechanics / Eds. P. Wriggers, W. Wagner*. Berlin: Springer, 1991.
179. E. A. Fancello and R. A. Feijoo, "Shape Optimization in Frictionless Contact Problems," *Intern. J. Numer. Meth. Engng.*, Vol. 37, No. 1-3, pp. 2311-2335, 1994.
180. E. A. Fancello, J. Haslinger, R. A. Feijoo, "Numerical Comparison Between Two Cost Functions in Contact Shape Optimization," *Structural Optimization*, Vol. 9, No. 1, pp. 57-68, 1995.
181. K. Farahani, M. Mofid, A. Vafai, "A solution method for general contact-impact problem," *Comput. Meth. Appl. Mech. Engng.*, Vol. 187, No. 1-2, pp. 69-77, 2000.
182. K. Farahani, M. Mofid, A. Vafai, "United Elements Method for General Contact-Impact Problems," *Comput. Methods Appl. Mech. Engng.*, Vol. 191, No. 8-10, pp. 843-860, 2001.
183. L. O. Faria, J. M. Bass, J. T. Oden, E. B. Becker, "A Three-Dimensional Rolling Contact Model for a Reinforced Rubber Tire," *Tire Sci. Technol.* Vol. 17, No. 3, pp. 217-233, 1989.
184. L. O. Faria, J. M. Bass, J. T. Oden, et al., "Tire Modelling by Finite Elements," *Tire Sci. Technol.*, Vol. 20, No. 1, pp. 33-56, 1992.
185. C. Farhat and F.-X. Roux F.-X. "A Method of Finite Element Tearing and Interconnecting and its Parallel Solution Algorithm," *Intern. J. Numer. Mech. Engng.*, Vol. 32, No. 6, pp. 1205-1227, 1991.
186. C. Farhat, L. Cruvelli, F.-X. Roux, "A Transient FETI Methodology for Large-Scale Parallel Implicit Computations in Structural Mechanics," *Intern. J. Numer. Meth. Engng.*, Vol. 37, No. 11, pp. 1945-1975, 1994.

187. C. Farhat, P.-S. Chen, J. Mandel, "A Scalable Lagrange Multiplier Based Domain Decomposition Method for Time-Dependent Problems," *Intern. J. Numer. Meth. Engng.*, Vol. 38, No. 22, pp. 3831–3853, 1995.
188. J. Farmer, L. Martinelli, A. Jameson, "Fast multigrid method for solving incompressible hydrodynamic problems with free surfaces. *AIAA J.*, Vol. 32, No. 6, 1994.
189. B. LaFaurie, C. Nardone, R. Scardovelly, S. Zaleski, "Modelling Merging and Fragmentation in Multi-phase Flows with SURFER," *J. Comput. Phys.*, Vol. 113, No. 1, pp. 134–147, 1994.
190. R. P. Fedorenko, A Method for Solving 3D Problems of Rolling with Slip and Adhesion [in Russian], Preprint No. 158, Institute of Applied Mathematics of the USSR Academy of Sciences, Moscow, 1979.
191. C. A. Felippa, K. C. Park, C. Farhat, "Partitioned Analysis of Coupled Mechanical Systems," Invited Plenary Lecture: 4th World Congr. Comput. Mech. Buenos Aires. Argentina. 1998; *Comput. Meth. Appl. Mech. Engrg.*, Vol. 190, No. 24–25, pp. 3247–3270, 2001.
192. R. J. Fennema and M. H. Chaudhry, "Implicit Methods for Two-Dimensional Unsteady Free-Surface Flows," *J. Hydraulic Research*, Vol. 27, No. 3, pp. 324–331, 1989.
193. G. Fikera, Existence Theorems in the Theory of Elasticity [Russian translation], Mir, Moscow, 1974.
194. J. Fish, Finite Element Method for Localization Analysis, Ph.D. thesis. Northwestern University, USA, 1989.
195. L. M. Flanagan and D. P. Flanagan, "PRONTO3D: A Three-Dimensional Transient Solid Dynamics Program," Tech. Rep. SAND87-1912, Sandia National Labs, Albuquerque, NM, 1989.
196. M. Fleming, Y. A. Chu, B. Moran, T. Belytschko, "Enriched Element-Free Galerkin Methods for Singular Fields," *Intern. J. Numer. Methods Engng.*, Vol. 40, No. 8, pp. 1483–1504, 1997.
197. J. M. Floryan and H. Rasmussen, "Numerical methods for viscous flows with moving boundaries," *Appl. Mech. Rev. (AMR)*, Vol. 42, No. 12, pp. 323–341, 1989.
198. V. M. Fomin and N. N. Yanenko, "Numerical simulation of high-speed interaction of bodies," in *Materials of the Symposium "Nonlinear Deformation Waves"* [in Russian], *In-t Kibernetiki AN ESSR*, Vol. 2, pp. 179–182, 1978.
199. V. M. Fomin, A. I. Gulidov, G. A. Sapozhnikov, et al., *High-speed Interaction of Bodies* [in Russian], *Izd-vo SO RAN*, Novosibirsk, 1999.
200. A. Francavilla and O. C. Zienkiewicz, "A Note on Numerical Computation of Elastic Contact Problems," *Intern. J. Numer. Methods Engng.*, Vol. 9, P. 913–924, 1975.
201. B. Fredriksson, "Finite Elements Solutions of Surface Nonlinearities in Structural Mechanics with Special Emphasis to Contact and Fracture Mechanics Problems," *Computers and Structures*, Vol. 6, pp. 281–290, 1976.
202. H. M. De La Fuente and C. A. Felippa, "Ephemeral penalty functions for contact dynamics," *Finite Elements in Analysis and Design*, Vol. 9, No. 3, pp. 177–191, 1991.
203. Y. C. Fung, *Biomechanics*. N.Y.: Springer, 1993.
204. I. I. Fuks, "One method for the numerical solution of 2D dynamic contact problems for elastoplastic bodies," in *Applied Problems of Strength and Plasticity* [in Russian], *Izd-vo Gor'kovskogo Universiteta*, Gorky, Issue 3, pp. 78–81, 1976.
205. M. A. Galakhov and P. P. Ussov, *Differential and Integral Equations of the Mathematical Theory of Physics* [in Russian], Nauka, Moscow, 1990.
206. L. A. Galin, "Indentation of a punch in the presence of friction and adhesion," *PMM [Applied Mathematics and Mechanics]*, Vol. 9, No. 5, pp. 413–424, 1945.
207. L. A. Galin, *Contact Problems of Elasticity* [in Russian], Gostekhizdat, Moscow, 1953.
208. L. A. Galin, *Contact Problems in the Theory of Elasticity*, Ed. I. N. Sneddon, North Carolina State College Translation, 1961.
209. L. A. Galin (ed.), *Development of the Theory of Contact Problems in the USSR* [in Russian], Nauka, Moscow, 1976.

210. L. A. Galin (ed.), *Contact Problems of Elasticity and Viscoelasticity* [in Russian], Nauka, Moscow, 1980.
211. J. Ghaboussi, E. L. Wilson, J. Isenberg, "Finite element of rock joints and Interfaces," *J. Soil Mech. and Foundat. Division, ASCE*. Vol. 99, N. 10, pp. 833–848, 1973.
212. A. E. Giannopolis, "The Return Mapping Method for the Integration of Friction Constitutive Equations," *Computers and Structures*, Vol. 32, pp. 157–168, 1989.
213. K. A. Gillow and S. D. Howison, *A bibliography on free and moving boundary problems for Hele-Shaw and Stokes Flow*, 2002.
Internet: <http://www.maths.ox.ac.uk/~howison/Hele-Shaw>.
214. A. N. Gil'manov, *Adaptive Grid Methods in Gas Dynamics* [in Russian], Nauka, Fizmatlit, Moscow, 2000.
215. R. A. Gingold and J. J. Monaghan, "Smoothed particle hydrodynamics: theory and applications," *Monthly Notices of the Royal Astronomical Society*, Vol. 181, pp. 375–389, 1977.
216. M. Ginsberg and J. P. Johnson, "Benchmarking the Performance of Physical Impact Simulation Software on Vector and Parallel Computers," *Proc. Supercomputing 88: V. 2. Science and Applications*. N.Y.: Computer Society Press, pp. 180–190, 1988.
217. M. Ginsberg and R. B. Katnik, "Improving Vectorization of a Crashworthiness Code," *SAE Techn. Paper No. 891985, Passenger Car Meeting and Explosion*, Dearborn, MI, 1989.
218. Yu. P. Glagoleva, V. M. Zhogov, Yu. F. Kir'yanov, et al., "Fundamentals of the Meduza technique," *Chislennye Metody Mekhaniki Splushnoi Sredy*, Vol. 3, No. 2, pp. 18–55, 1973.
219. J. Glimm, J. W. Grove, X. L. Li, N. Zhao, "Simple Front Tracking," *Contemporary Math.*, 1999, Vol. 238. pp. 133–149, 1999.
Internet: <http://www.mie.utoronto.ca/labs/tsl/pubs/pof.bussmann.pdf>
220. F. Pfeiffer and Ch. Glocker, *Multibody dynamics with unilateral contacts*. N.Y.: Wiley, 1996.
221. Ch. Glocker, "Formulation of spatial contact situations in rigid multibody systems," *Comput. Meth. Appl. Mech. Engng.*, Vol. 177, No. 3–4, pp. 199–214, 1999.
222. B. L. Glushak, S. A. Novikov, A. I. Ruzanov, and A. I. Sadyrin, *Fracture of Deformable Media under Impulsive Loads* [in Russian], Izd-vo Nizhegorodskogo Universiteta, Nizhny Novgorod, 1992.
223. S. K. Godunov, "A difference method for numerical construction of discontinuous solutions of hydrodynamics equations," *Matematicheskii Sbornik*, Vol. 47, No. 3, pp. 271–306, 1959.
224. S. K. Godunov and G. P. Prokopov, "On the utilization of movable grids in gas dynamics calculations," *Zhurnal Vychislitel'noi Matematiki i Matematicheskoi Fiziki* [Journal of Computational Mathematics and Mathematical Physics], Vol. 12, No. 2, pp. 429–440, 1972.
225. S. K. Godunov, A. V. Zabrodin, M. Ya. Ivanov, et al., *Numerical Solution of Multidimensional Problems of Gas Dynamics* [in Russian], Nauka, Moscow, 1976.
226. R. V. Goldstein, A. F. Zazovskii, A. A. Spektor, and R. P. Fedorenko, *Solution of 3D Contact Problems of Rolling with Slip and Adhesion by a Variational Method* [in Russian], Preprint No. 134, Institute for Problems in Mechanics of the Russian Academy of Sciences, Moscow, 2004.
227. R. V. Goldstein and A. A. Spektor, "Variational methods for solution and investigation of 3D contact and mixed problems with friction," in *Mechanics of a Deformable Body* [in Russian], Nauka, Moscow, 1986, pp. 52–73.
228. V. A. Gorel'skii, I. E. Khorev, and N. T. Yugov, "Numerical analysis of 3D problems of indentation and fracture of cylinders under an asymmetric load," *Fizika Goreniya i Vzryva*, No. 1, pp. 71–74, 1987.
229. V. A. Gorel'skii and A. V. Radchenko, "Kinetics of fracture of a two-layered plate subjected to a shock wave load," *Prikladnaya Mekhanika*, Vol. 27, No. 11, 1991.
230. V. A. Gorel'skii, S. A. Zelepugin, V. N. Sidorov, "Numerical investigation of a 3D problem of interaction of a filled shaped projectile with a high-strength target," *Problemy Prochnosti*, No. 1, pp. 47–50, 1992.

231. A. V. Gorodnichev, G. P. Simonov, Yu. V. Yanilkin, "EGAK-EP method for calculations of fracture and fragmentation of materials," in *New Models and Numer. Codes for Shock Wave Processes in Condensed Media*. Oxford, 1997.
232. A. G. Gorshkov and D. V. Tarlakovskii, *Dynamic Contact Problems with Moving Boundaries* [in Russian], Nauka, Fizmatlit, Moscow, 1995.
233. A. G. Gorshkov and D. V. Tarlakovskii, "Unsteady dynamic contact problems," in *Mechanics of Contact Interactions* [in Russian], I. I. Vorovich and V. M. Alexandrov (eds.), Nauka, Fizmatlit, Moscow, 2001, pp. 349–416.
234. I. G. Goryacheva and M. N. Dobychin, *Contact Problems in Tribology* [in Russian], Mashinostroenie, Moscow, 1988.
235. I. G. Goryacheva and M. N. Dobychin, "Multiple contact model in the problem of tribomechanics," *Tribology Intern.*, Vol. 24, No. 1, pp. 29–35, 1991.
236. I. G. Goryacheva, *Contact Mechanics in Tribology*. Kluwer, Dordrecht etc., 1998.
237. I. G. Goryacheva and O. G. Chekina, "Mechanics of discrete contact," in *Mechanics of Contact Interactions* [in Russian], I. I. Vorovich and V. M. Alexandrov (eds.), Nauka, Fizmatlit, Moscow, pp. 418–437, 2001.
238. G. L. Goudreau and J. O. Hallquist, "Recent developments in large-scale finite element Lagrangian hydrocode technology," *Comput. Meth. Appl. Mech. Engng.*, Vol. 33, pp. 725–757, 1982.
239. J.-P. Gourret, N. M. Thalmann, D. Thalmann, "Simulation of object and human skin deformations in a grasping task," *Proc. SIGGRAPH 89. Computer Graphics*, Vol. 23, No. 3, pp. 21–30, 1989.
240. E. I. Grigolyuk and A. G. Gorshkov, "Interaction of Elastic Structures with a Fluid," *Sudostroenie*, Leningrad, 1976.
241. E. I. Grigolyuk and V. M. Tolkachev, *Contact Problems of the Theory of Plates and Shells* [in Russian], Mashinostroenie, Moscow, 1980.
242. S. S. Grigoryan (editor), *Dynamics of Impact* [in Russian], Mir, Moscow, 1985.
243. V. A. Gridneva, A. I. Korneev, and V. G. Trushkov, "Numerical calculation of the stress state and fracture of a finite-thickness plate impacted by projectiles of various shapes," *Izv. AN SSSR. MTT [Mechanics of Solids]*, No. 1, pp. 146–157, 1991.
244. V. A. Gridneva and M. M. Nemirovich-Danchenko, "A method of separation of grid points for numerical calculation of fracture of solids," *Tomskii Univrsitet*, Tomsk, Registered VINITI No. 3258-83, 1983.
245. F. M. Guerra and R. V. Browning, "Comparison of two slideline methods using ADINA," *Computers and Structures*, Vol. 17, No. 5/6, pp. 819–834, 1983.
246. D. Gueyffier, J. li, A. Nadim, R. Scardovelli, S. Zaleski, "Volume- of-Fluid Interface Tracking with Smoothed Surface Stress Methods for Three Dimensional Flows," *J. Comput. Phys.*, Vol. 152, pp. 423–456, 2000.
247. A. I. Gulidov and V. M. Fomin, *A Modification of the Wilkins Method for Solving Body Collision Problems* [in Russian], Preprint No. 49, ITPM SO AN SSSR, Novosibirsk, 1980.
248. A. I. Gulidov, "Penetration of a rigid impactor into a deformable target," in *Numerical Methods for Solving Problems of Elasticity and Plasticity. Materials of the 6th All-Union Conf.* [in Russian], ITPM SO AN SSSR, Novosibirsk, Part 1, pp. 59–69, 1980.
249. A. I. Gulidov, V. M. Fomin, and I. I. Shabalin, "An algorithm for the reconstruction of the difference grid for numerical solution of problems of collision with crack formation," in *Numerical Methods for Solving Problems of Elasticity and Plasticity. Materials of the 7th All-Union Conf.* [in Russian], ITPM SO AN SSSR, Novosibirsk, pp. 182–192, 1982.
250. A. I. Gulidov, V. M. Fomin, and I. I. Shabalin, "Numerical simulation of an impact of two bodies with fracture," in *Numerical Solution of Physical and Mechanical Problems of Strength. All-Union Conf. Abstracts of Papers* [in Russian], Gorky, p. 60, 1983.
251. A. I. Gulidov and I. I. Shabalin, *Numerical Formulation of Boundary Conditions in Dynamic Contact Problems* [in Russian], Preprint No. 12–87, ITPM SO AN SSSR, Novosibirsk, 1987.

252. A. I. Gulidov and I. I. Shabalin, "Calculation of contact boundaries for dynamic interaction of deformable bodies with friction being taken into account," in *Numerical Methods for Solving Problems of Elasticity and Plasticity. Materials of the 10th All-Union Conf.* [in Russian], ITPM SO AN SSSR, Novosibirsk, pp. 70–75, 1988.
253. A. I. Gulidov and I. I. Shabalin, *Free Element Method* [in Russian], Preprint No. 9–94, ITPM SO AN SSSR, Novosibirsk, 1994.
254. A. I. Gulidov and I. I. Shabalin, "Free-element simulation of the process of penetration of rods into massive targets," in *Numerical Methods for Solving Problems of Elasticity and Plasticity. Materials of the 13th Inter-republican Conf.* [in Russian], ITPM SO AN SSSR, Novosibirsk, pp. 68–76, 1995.
255. F. C. Gunther and W. K. Liu, "Implementation of Boundary Conditions for Meshless Methods," *Comput. Meth. Appl. Mech. Engng.*, Vol. 163, No. 1–4, pp. 265–230, 1998.
256. J. O. Hallquist, *A Procedure for the Solution of Finite Deformation Contact-Impact Problems by the Finite Element Method*, Univ. of California, Lawrence Livermore National Laboratory, Rept. UCRL-52066. 1976.
257. J. O. Hallquist, *Preliminary User's Manuals for DYNA3D and DYNAP (Nonlinear Dynamic Analysis of Solids in Three Dimension)*, Univ. of California, Lawrence Livermore National Laboratory, Rept. UCID-17268. 1976.
258. J. O. Hallquist, "A numerical treatment of sliding interfaces and impact," *Comput. Techniques for Interface Problems / Eds. K. C. Park, D. K. Gartling, AMD, ASME*, Vol. 30, pp. 117–133, 1978.
259. J. O. Hallquist, *Theoretical Manual for DYNA3D*, Lawrence Livermore National Laboratory, Rept. UCID-19401, 1983.
260. J. O. Hallquist, G. L. Goudreau, D. J. Benson, "Sliding interfaces with contact-impact in large-scale Lagrangian computation," *Comput. Meth. Appl. Mech. Engng.*, Vol. 51, No. 1–3, pp. 107–137, 1985.
261. J. O. Hallquist, K. Schweizerhof, D. Stillman, "Efficiency Refinements of Contact Strategies and Algorithms in Explicit FE Programming," *Proc. COMPLAS 3 / Eds. D. R. J. Owen, E. Hinton, E. E. Onate*, Pineridge Press, 1992.
262. J. O. Hallquist, *LS-DYNA Theoretical Manual*, Livermore Software Technology Corporation, 1998.
263. W. Han and M. Sofonea, "On Numerical Approximation of a Frictionless Contact Problem for Elasto-Viscoplastic Materials," *Integral Methods in Science and Engineering / Eds. B. Bertram et al. Chapman and Hall / CRC Research Notes in Mathematics. Vol. 418*, pp. 173–178, 2000.
264. W. Han and M. Sofonea, "Numerical analysis of quasistatic viscoelastic problem with friction and damage," *Advances in Scientific Computing. / Eds. Zhong-ci Shi et al. Beijing; New York: Science Press*, pp. 51–60, 2001.
265. F. H. Harlow and J. E. Welch, "Numerical calculation of time-dependent viscous incompressible flow of fluid with free surface," *Phys. Fluids.*, Vol. 8, No. 12, pp. 2182–2198, 1965.
266. F. H. Harlow and J. P. Shannon, "The splash of a liquid drop," *J. Appl. Phys.*, Vol. 38, p. 3855, 1967.
267. F. H. Harlow, "The particle-in-cell numerical method for problems of hydrodynamics," in *Numerical Methods in Hydrodynamics [Russian translation]*, B. Older (ed.), Mir, Moscow, pp. 316–342, 1967.
268. F. H. Harlow and A. A. Amsden, "Numerical simulation of almost incompressible flow," *J. Comput. Phys.*, 1968, Vol. 3, p. 80, 1968.
269. F. H. Harlow and J. E. Welch, "Numerical calculation of time-dependent viscous incompressible flow with free boundaries," *Phys. Fluids*, Vol. 8, p. 2182, 1968.
270. F. Harlow and A. Amsden, "Flow of Interpenetrating Material Phases," *J. Comput. Phys.*, Vol. 18, 1975.
271. E. J. Haug and B. M. Kwak, "Contact Stress Minimization by Contour Design," *Intern. J. Numer. Meth. Engng.*, Vol. 12, No. 6, pp. 917–930, 1978.
272. J.-H. Heegaard and A. Cournier, "An Augmented Lagrangian method for discrete large-slip contact problems involving friction," *Intern. J. Numer. Meth. Engng.*, Vol. 36, No. 4, pp. 569–593, 1993.

273. M. W. Heinstein and T. A. Laursen “An Algorithm for the Matrix-Free Solution of Quasistatic Frictional Contact Problems,” *Intern. J. Numer. Meth. Engng.*, Vol. 44, No. 9, pp. 1205–1226, 1999.
274. M. W. Heinstein, F. J. Mello, S. W. Attaway, T. A. Laursen, “Contact-Impact Modeling in Explicit Transient Dynamics,” *Comput. Meth. Appl. Mech. Engng.*, Vol. 187, No. 3–4, pp. 621–640, 2000.
275. H. Hertz, “Uber die Berührung fester elastischer Korper,” *J. Reine Angew. Math.*, Bd. 92, s. 156–171, 1882.
276. M. R. Hestenes and E. Stiefel, “Method of conjugate gradients for solving linear systems,” *J. Res. Nat. Bur. Std.*, Vol. 49, No. 6, pp. 409–436, 1952.
277. Hibbit, Karksson, Sorensen, ABAQUS Theory Manual. ver. 5.8, 1998.
278. T. Hino, “An unstructured grid method for incompressible viscous flows with a free surface,” AIAA Paper N. 97-0862, 1997.
279. S. Hirokawa and R. Tsuruno, “Three-dimensional deformation and stress distribution in an analytical computational model of the interior cruciate ligament,” *J. Biomechanics*, Vol. 33, No. 9, pp. 1069–1077, 2000.
280. G. Hirota, S. Fisher, A. State, C. Lee, H. Fuchs, “An Implicit Finite Element Method for Elastic Solids in Contact,” SIGGRAPH 2001 Conf. 2001.
Internet: <http://www.cs.unc.edu/~hirota/fem/hirota2002.pdf>
http://www.cs.unc.edu/~andrei/pubs/2001_ComputerAnimation_FEM.pdf
281. C. W. Hirt, “Arbitrary Lagrangian Eulerian method,” *Proc. 2nd Intern. Conf. Numer. Meth. Fluid Dynamics.* / Ed. Maurice Holt. Berkeley: Univ. of California. Berlin, Heidelberg, New York: Springer, 1971.
282. C. W. Hirt, A. A. Amsden, and J. L. Cook, “An arbitrary Lagrangian-Eulerian computing method for all flow speeds,” *J. Comput. Phys.*, Vol. 135, p. 203, 1997, reprinted from *J. Comput. Phys.*, Vol. 14, p. 227, 1974.
283. C. W. Hirt and B. D. Nickols, “Volume of Fluid (VOF) method for the dynamics of free boundaries,” *J. Comput. Physics*, Vol. 39, No. 1, pp. 201–225, 1981.
284. I. Hlavacek, J. Haslinger, J. Necas, J. Lovisek, *Solution of variational inequalities in mechanics*, New York: Springer, 1988.
285. C. G. Hoover, D. C. Badders, A. J. De Groot, R. J. Sherwood, *Parallel algorithm research for solid mechanics applications using finite element analysis*, Thrust Area Report, UCRL-ID-125471, Lawrence National Laboratory, 1997.
286. T. J. R. Hughes, R. L. Taylor, J. L. Sackman, et al., “A finite element method for a class of contact-impact problems,” *Comput. Meth. Appl. Mech. Engng.*, Vol. 8, pp. 249–276, 1976.
287. T. J. R. Hughes, R. L. Taylor, W. Kanoknukulchai, “A finite element method for Large Displacement Contact and Impact Problems,” *Formulations and Computational algorithms in FE Analysis* / Ed. K. J. Bathe. Boston: MIT-Press, pp. 468–495, 1977.
288. T. J. R. Hughes, “Analysis of transient algorithms with particular reference to stability behavior,” *Computational Methods for Transient Analysis* / Eds. T. Belytschko, T. J. R. Hughes. North-Holland, pp. 67–155, 1983.
289. T. J. R. Hughes, *The Finite Element Method*, Prentice-Hall, New York, 1987.
290. G. J. Huh and B. M. Kwak, “Constrained variational approach for dynamic analysis of elastic contact problems,” *Finite Elem. Anal. and Des.*, Vol. 10, No. 2, pp. 125–136, 1991.
291. I. Hunek, “On a penalty formulation for contact-impact problems,” *Computers and Structures*, Vol. 43, No. 2, pp. 193–203, 1993.
292. J. M. Hyman, “Numerical methods for tracking interfaces,” *Physica*, Vol. 12, No. 1–3, pp. 396–407, 1984.
293. A. R. Ingraffea and F. E. Heuze, “Finite element models for rock fracture mechanics,” *Intern. J. Numer. Anal. Meth. Geomech.*, Vol. 4, No. 1, pp. 25–43, 1980.

294. S. A. Ivanenko, Adaptive-harmonic Grids [in Russian], Computing Center of the Russian Academy of Sciences, Moscow, 1997.
295. S. A. Ivanenko, "A barrier method for the construction of quasi-harmonic grids," *Zhurnal Vychislitel'noi Matematiki i Matematicheskoi Fiziki* [Journal of Computational Mathematics and Mathematical Physics], Vol. 40, No. 11, pp. 1600–1616, 2000.
296. K. B. Ivashchenko, "Calculation of contact boundaries in problems of in Dynamic Problems of Continuum Mechanics." Regional Conf. Abstracts of Papers [in Russian], KubGU, Krasnodar, Part 1, pp. 59–61, 1988.
297. K. B. Ivashchenko, "An algorithm for calculation of the contact boundaries in the case of interaction of solid bodies," *Problemy Prochnosti*, No. 2, pp. 79–82, 1989.
298. D. Jacqmin, "A variational approach to deriving smeared interface surface tension models," *Barriers and Challenges in CFD* / Ed. V. Venkatakrishnan et al. Dordrecht-Nowell, MA, Kluwer Academic, pp. 231, 1998.
299. M. Jaeger and M. Carin, "The Front-Tracking ALE Method: Application to a Model of the Freezing of Cell Suspensions," *J. Comput. Phys.*, Vol. 179, pp. 704II-735, 2002.
300. A. Jagota and S. J. Bennison, "Element breaking rules in computational models for brittle fracture," *Modelling Simul. Mater. Sci. Engng.*, Vol. 3, pp. 485–501, 1995.
301. M. Jean, "Unilateral contact and dry friction: time and space discrete variables formulation," *Arch. Mech.*, Vol. 40, pp. 677–691, 1988.
302. M. Jean, "Frictional contact in rigid or deformable bodies," *Numerical simulations of geomaterials*. Amsterdam: Elsevier, pp. 463–486, 1995.
303. M. Jean, "The nonsmooth contact dynamics method." *Comput. Meth. Appl. Mech. Engng.*, Vol. 177, pp. 235–257, 1999.
304. J. O. Jim and B. M. Kwak, "Dynamic analysis of two-dimensional frictional contact by linear complementarity problem formulation," *Intern. J. Solids and Structures*, Vol. 33, No. 30, pp. 4605–4624, 1996.
305. P. K. Jimack, "Adaptive Algorithms for Free-Surface Flow Problems," *The 4th Intern. Conf. on Engng Comput. Techn.* Lisbon. 2004.
Internet: www.scs.leeds.ac.uk/pkj/Papers/Conf-I/J04.pdf
306. L. Johanson and A. Klarbring, "Thermoelastic Frictional Contact Problems: Modelling, Finite Element Approximation and Numerical Realization," *Comput. Meth. Appl. Mech. Engng.*, Vol. 105, pp. 181–210. 1993.
307. A. A. Johnson and T. E. Tezduyar, "Mesh updated strategies in parallel finite element computations of flow problems with moving boundary and interface," *Comput Meth. Appl. Mech. Engng.*, Vol. 119, pp. 73–94, 1994.
308. C. Johnson, "Adaptive finite element methods for the obstacle problem," *Technical Report*. Goteborg: Chalmers University of Technology, 1991.
309. C. Johnson and P. Hansbo, "Adaptive finite element methods in computational mechanics," *Comput. Meth. Appl. Mech. Engng.*, Vol. 101, pp. 143–181, 1992.
310. G. R. Johnson, "Analysis of elastic-plastic impact involving severe distortions," *Trans. ASME, J. Appl. Mech.*, Vol. 43, No. 3, pp. 439–444, 1976.
311. G. R. Johnson, "High velocity impact in three dimensions," *Trans. ASME, J. Appl. Mech.*, Vol. 44, No. 1, pp. 95–100, 1977.
312. G. R. Johnson and R. A. Stryk, "Eroding interface and improved tetrahedral element algorithms for high-velocity impact computations in three dimensions," *Intern. J. Impact Engng.*, Vol. 5, No. 1–4, pp. 411–421, 1987.
313. G. R. Johnson and R. A. Stryk, "Recent EPIC code developments for high velocity impact," *Int. J. Impact Engng.*, Vol. 10, No. 1–4, pp. 281–294, 1990.
314. K. L. Johnson, *Contact Mechanics*. Cambridge: Univ. Press, 1985.

315. N. L. Johnson, "Legacy and future of CFD at Los Alamos," Canadian CFD Conf., Technical Report No. LA-UR-96-1426, pp. 1-20, Los Alamos National Lab., Ottawa, 1996.
Internet: http://gnarly.lanl.gov/History/CFD_paper_6_24_96.pdf
<http://t3.lanl.gov/secondlevel/history/viewgraphs.pdf>.
316. J. W. Ju, R. L. Taylor, L. Y. Cheng, "A consistent finite element formulation of nonlinear frictional contact problems," Numerical Techniques for Engineering Analysis and Design / Eds. G. N. Pande and J. Middleton. Nijhoff Publ., Dordrecht, pp. D5/1-D5/13, 1987.
317. J. W. Ju and R. L. Taylor, "A perturbed lagrangian formulation for the finite-element solution of nonlinear frictional contact problems," J. de Mec. Theor. et Appl., 1988. Vol. 7, No. 1, pp. 1-14, 1988.
318. L. Jun and D. B. Spalding, "Numerical simulation of flows with moving interfaces," PHOENICS J. Comput. Fluid Dynamics, Vol. 10, No. 5/6, pp. 625-637, 1988.
319. I. Kaljevic and S. Saigal, "An Improved Element Free Galerkin Formulation," Intern. J. Numer. Meth. Engng., Vol. 40, No. 16, pp. 2953-2974, 1997.
320. J. J. Kalker and Y. Randen, "A Minimum Principle for Frictionless Elastic Contact with Application to non-Hertzian Half-Space Contact Problems," J. Engng. Math., Vol. 6, No. 2, pp. 193-206, 1972.
321. J. J. Kalker, Three-Dimensional Elastic Bodies in Rolling Contact, Kluwer, Dordrecht, 1990.
322. S. G. Kalmykov and V. N. Kukudzhanov, Flow and Correction Marker Method for Numerical Simulation of High-speed Impacts of Solids [in Russian], Preprint No. 529, Institute for Problems in Mechanics of the Russian Academy of Sciences, Moscow, 1993.
323. C. Kane, E. A. Repetto, M. Ortiz, J. E. Marsden, "Finite element analysis of nonsmooth contact," Comput. Meth. Appl. Mech. Engng., Vol. 180, No. 1-4, pp. 1-26, 1999.
324. C. Kane, J. E. Marsden, M. Ortiz, M. West, "Variational integrators and the newmark algorithm for conservative and dissipative mechanical systems," Intern. J. Numer. Meth. Engng., Vol. 49, No. 10, pp. 1295-1325, 2000.
325. Y. Kanto and G. Yagawa, "A dynamic contact buckling analysis by the penalty finite element method," Intern. J. Numer. Meth. Engng., Vol. 29, No. 4, pp. 755-774, 1990.
326. H. Kardestuncer and D. H. Norrie (Editors), Finite Element Handbook, McGraw Hill, N.Y., 1987.
327. S. Karni, "Multicomponent flow calculation by a consistent primitive algorithm," J. Comput. Phys., Vol. 112, pp. 31, 1994.
328. S. W. Key, HONDO - A Finite Element Computer Program for the Large Deformation Response of Axisymmetric Solids. Sandia National Labs. Report 74-0039. 1974.
329. N. Kikuchi and Y. J. Song, "Penalty finite element approximations of a class of unilateral problems in linear elasticity," Quaterly of Appl. Mech., Vol. 39, No. 1, pp. 1-21, 1981.
330. N. Kikuchi, "A smoothing technique for reduced integration penalty methods in contact problems," Intern. J. Numer. Meth. Engng., Vol. 18, No. 3, pp. 343-350, 1982.
331. N. Kikuchi and J. T. Oden, "Contact Problems in Elasticity: A study of variational inequalities and finite element methods," in SIAM Studies in Appl. Math., Vol. 8, Philadelphia, 1988.
332. A. B. Kiselev, "Development of the Wilkins method for solving 3D impact problems for solids," in Interaction of Waves in Deformable Media [in Russian], Izd-vo MGU, Moscow, pp. 87-100, 1984.
333. A. B. Kiselev, "To the calculation of a 3D impact of an elastoplastic rod with a rigid obstacle," Vestnik MGU [Bulletin of the Moscow State University]. Mat. Mekh., No. 2, pp. 30-36, 1988.
334. A. B. Kiselev, "Numerical 3D simulation of skew breaking through thin obstacles," in Numerical Solution of Wave Dynamics Problem: Mathematical Studies [in Russian], Shtiintsa, Kishinev, Issue 108, pp. 19-26, 1989.
335. A. B. Kiselev and N. E. Kabak, "A method for constructing numerical grids with separation of internal contact boundaries," Modelirovanie v Mekhanike, Vol. 4, No. 5, pp. 96-110, 1990.
336. A. B. Kiselev, "Computational simulation of boundary conditions in problems of elastoplastic bodies interaction," Systems Analysis Modelling Simulation, Vol. 18-19, pp. 809-812, 1995.

337. A. Klarbring, "A Mathematical Programming approach to Three-dimensional Contact Problems with Friction," *Comput. Meth. Appl. Mech. Engng.*, Vol. 58, pp. 175–200, 1986.
338. A. Klarbring and G. Bjorkman, "A mathematical programming approach to contact problems with friction and varying contact surface," *Computer and Structures*, Vol. 30, No. 5, pp. 1185–1198, 1988.
339. A. Klarbring, "Examples of non-uniqueness and non-existence of solutions to quasistatic contact problem with friction," *Ingenieur Archiv*, Vol. 50, pp. 529–541, 1990.
340. A. Klarbring and G. Bjorkman, "Solution of Large Displacement Contact Problems with Friction using Newton's Method for Generalized Equations," *Intern. J. Numer. Meth. Engng.*, Vol. 34, pp. 249–269, 1992.
341. A. Klarbring, A. Mikelic, M. Shillor, "A global existence result for the quasistatic frictional contact problem with normal compliance," *Intern. Series Numer. Math.*, Vol. 101, pp. 85–111, 1992.
342. S. M. Klisch and J. C. Lotz, "Application of a fiber-reinforced continuum theory to multiple deformations of the annulus fibrosus," *J. Biomechanics*, Vol. 32, No. 10, pp. 1027–1036, 1999.
343. R. M. Koch, M. H. Gross, F. R. Carls, et al., "Simulating facial surgery using finite element methods," *Proc. SIGGRAPH '96. Computer Graphics. Annual Conference Series*, pp. 421–428, 1996.
344. V. I. Kondaurov and V. N. Kukudzhakov, "On the constitutive equations and numerical solution of some problems of dynamics of an elastoplastic medium subject to finite strains," in *Collected Papers on Numerical Methods in Solid Mechanics [in Russian]*, Computing Center of the USSR Academy of Sciences, Moscow, 1978, pp. 84–121.
345. V. I. Kondaurov and V. N. Kukudzhakov, "On constitutive equations and numerical solution of the multidimensional problems of the dynamics of nonisothermic elastic media with finite deformations," *Arch. Mech.*, Vol. 31, No. 5, pp. 623–647, 1979.
346. V. I. Kondaurov and V. N. Kukudzhakov, "Impact of a rigid cylinder against a laminated elastoplastic obstacle," in *Numerical Method for Solving Problems of Elasticity and Plasticity. Materials of the 6th All-Union Conference [in Russian]*, ITPM SO AN SSSR, Novosibirsk, pp. 84–90, 1980.
347. V. I. Kondaurov and I. B. Petrov, "Numerical study of the indentation of a rigid cylinder into an elastoplastic obstacle," in *Numerical Methods in Solid Mechanics [in Russian]*, Computing Center of the USSR Academy of Sciences, Moscow, pp. 115–132, 1984.
348. V. I. Kondaurov, I. B. Petrov, A. S. Kholodov, "Numerical simulation of the indentation of a rigid body of revolution into an elastoplastic obstacle," *PMTF*, No. 4, pp. 132–139, 1984.
349. V. I. Kondaurov and I. N. Lomov, "Fracture of brittle material with initial porosity under high energy density flows," *Shock Compression of Condensed Matter. / Ed. S. C. Smidt, Amer. Phys. Soc.*, pp. 247–250, 1998.
350. V. I. Kondaurov, "A tensor model of continuum fracture and long-term strength of elastic bodies," *Izv. RAN. MTT [Mechanics of Solids]*, No. 5, pp. 134–151, 2001.
351. V. I. Kondaurov, "Thermomechanics of Phase Transitions of the First Order in Solids," *Russian J. Earth Sci.*, Vol. 4, No. 2, pp. 1–18, 2002.
352. A. I. Korneev and A. P. Nikolaev, "Finite-element calculation of elastoplastic flow in the case of impact," *Tomskii Univrsitet, Tomsk, Registered VINITI*, No. 2137-80, 1980.
353. A. I. Korneev, A. P. Nikolaev, and I. E. Shipovskii, "Application of the finite-element method to problems of impact of solids," in *Numerical Method for Solving Problems of Elasticity and Plasticity. Materials of the 7th All-Union Conference [in Russian]*, ITPM SO AN SSSR, Novosibirsk, pp. 122–129, 1982.
354. A. I. Korneev and V. B. Shugalev, "Numerical calculation of 3D stress state of the rod in the case of impact by part of its lateral surface," *Izv. AN SSSR. MTT [Mechanics of Solids]*, No. 1, pp. 189–192, 1986.
355. S. N. Korobeinikov, V. V. Alyokhin, M. I. Bondarenko, "Application of a finite element method for the solution of three dimensional contact problems," *Advances in Simulation and Interaction Techniques: Proc. 2nd Intern. Conf. on Comput. Structures Technology / Eds. M. Papadrakakis, and B. H. V. Topping*, pp. 165–175, Civil-Comp. Press, Edinburgh, 1994.

356. S. N. Korobeinikov, *Nonlinear Deformation of Solids* [in Russian], Izd-vo SO RAN, Novosibirsk, 2000.
357. V. D. Koshur and S. A. Mart'yanov, "Homogeneous, through-calculation, symmetric algorithm for the numerical simulation of dynamic contact interaction of deformable bodies," in *Numerical Method for Solving Problems of Elasticity and Plasticity. Materials of the 12th All-Russian Conference* [in Russian], ITPM SO RAN, Novosibirsk, pp. 142–147, 1992.
358. D. B. Kothe and W. J. Rider, "Comments on modelling interfacial flows with volume-of-fluid method," Technical report LA-UR-3384, Los Alamos National Lab., 1994.
Internet: <http://www.c3.lanl.gov/~vjr/pubs.html>.
359. D. B. Kothe, W. J. Rider, S. J. Mosso, J. S. Brock, "Volume tracking of interfaces having surface tension in two and three dimensions," AIAA Paper N. 96-0859, 1996.
360. D. Kothe, D. Juric, K. Lam, B. Lally, Numerical recipes for mold filling simulation, Rept. N. 87545, Los Alamos National Laboratory, Los Alamos, USA, 1998.
Internet: www.lanl.gov/energy/est/transportation/trans/pdfs/materials/NUMREC.PDF
361. V. M. Kovenya and N. N. Yanenko, *Splitting Method in Gas Dynamics* [in Russian], Nauka, Novosibirsk, 1981.
362. P. Kowalczyk, "Finite-deformation interface formulation for frictionless contact problems," *Comm. Numer. Meth. Engng.*, Vol. 10, pp. 879–893, 1994.
363. I. V. Kragelsky, M. N. Dobychin, V. S. Kombalov, *Friction and Wear - Calculation Methods*, Pergamon Press, 1982.
364. A. S. Kravchuk and V. A. Vasil'ev, "Numerical methods for solving the contact problem for linearly and nonlinearly elastic bodies of finite dimension," *Prikladnaya Mekhanika*, Vol. 16, No. 6, pp. 9–15, 1980.
365. A. S. Kravchuk, "On the theory of contact problems with friction on the contact surface being taken into account," *PMM [Applied Mathematics and Mechanics]*, Vol. 44, No. 1, pp. 122–129, 1980.
366. A. S. Kravchuk, "Solution of some 3D contact problems with friction on the contact surface being taken into account," *Trenie i Iznos*, Vol. 2, No. 4, pp. 589–595, 1981.
367. A. S. Kravchuk, "Solution of contact problems with known Green's function," *PMM [Applied Mathematics and Mechanics]*, Vol. 46, No. 2, pp. 283–288, 1982.
368. A. S. Kravchuk and E. R. Akhundzhanov, "Numerical version of the variational approach to the solution of contact problems of elasticity by the potential method," in *Strength Analysis* [in Russian], Issue 25, pp. 12–18, Mashinostroenie, Moscow, 1983.
369. A. S. Kravchuk, "Solution of nonlinear contact problems with friction by variational methods," in *Mechanics and Progress in Science and Technology. Volume 3. Solid Mechanics* [in Russian], pp. 154–169, Nauka, Moscow, 1988.
370. A. S. Kravchuk, *Variational and Quasi-variational Inequalities in Mechanics* [in Russian], Mosk. Gos. Akad. Priborostroeniya i Informatiki, Moscow, 1997.
371. A. S. Kravchuk, "Method of variational inequalities for contact problems," in *Mechanics of Contact Interaction* [in Russian], I. I. Vorovich and V. M. Alexandrov (eds.), pp. 93–115, Fizmatlit, Moscow, 2001.
372. V. D. Kubenko, *Penetration of Elastic Shells into a Compressible Fluid* [in Russian], Naukova Dumka, Kiev, 1981.
373. V. D. Kubenko, "Impact interaction of bodies with the environment. A review," *Prikladnaya Mekhanika*, Vol. 33, No. 12, pp. 3–29, 1997.
374. V. N. Kukudzhanov, "Numerical simulation of dynamic processes of deformation and fracture in elasto-plastic media," *Uspekhi Mekhaniki [Advances in Mechanics]*, Vol. 8, No. 4, pp. 21–65, 1985.
375. V. N. Kukudzhanov, N. G. Bourago, A. N. Kovshov, et al., On the problem of damage and localization of strains, Preprint No. 95:11, pp. 1–35, Chalmers Univ. of Technol., Dept. Struct. Mech., Goteborg, 1995.
Internet: <http://www.ipmnet.ru/~burago/papers/grid.htm>.

376. V. N. Kukudzhanov and K. Santaoja, "Thermodynamics of viscoplastic media with internal parameters," *Izv. RAN. MTT [Mechanics of Solids]*, No. 2, pp. 115–126, 1997.
377. R. F. Kulak, "Adaptive contact elements for three-dimensional explicit transient analysis," *Comput. Meth. Appl. Mech. Engng.*, Vol. 72, pp. 125–151, 1989.
378. A. G. Kulikovskii, N. V. Pogorelov, A. Yu. Semenov, *Mathematical Aspects of Numerical Solution of Hyperbolic systems*, Chapman Hall, London, Boca Raton, 2001.
379. A. G. Kulikovskii, N. V. Pogorelov, and A. Yu. Semenov, *Mathematical Issues of the Numerical Solution of Hyperbolic Systems of Equations [in Russian]*, Fizmatlit, Moscow, 2001.
380. T. Kunugi, MARS for multiphase flow, Kyoto Univ., pp. 1–10, 2002.
Internet: www.nucleng.kyoto-u.ac.jp/Groups/F-group/gallery/pdf/isofd13.pdf
381. A. G. Kuz'menko, *Fundamental Equations of Elasticity and Plasticity and the Finite-element Method [in Russian]*, Tul'skii Politekhnikeskii Institut, Tula, 1980.
382. A. L. Kvitka, P. P. Voroshko, and S. D. Bobtitskaya, *Stress-strain State of Bodies of Revolution [in Russian]*, Naukova Dumka, Kiev, 1977.
383. B. M. Kwak, "Complementary problem formulation of three-dimensional frictional contact," *J. Appl. Mech.*, *Trans. ASCE*, Vol. 58, pp. 134–140, 1991.
384. P. Ladeveze, *Nonlinear Computational Structural Mechanics*. Springer, N.Y., 1998.
385. R. Larsson and R. Runesson "Discontinuous displacement approximation for capturing plastic localization," *Intern. J. Numer. Meth. Engng.*, Vol. 36, No. 12, pp. 2087–2105, 1993.
386. T. A. Laursen and J. C. Simo, "Algorithmic Symmetrization of Coulomb Frictional Problems Using Augmented Lagrangians," *Comput. Meth. Appl. Mech. Engng.*, Vol. 108, No. 1/2, P. 133–146, 1993.
387. T. A. Laursen and J. C. Simo, "A Continuum-Based Finite Element Formulation for the Implicit Solution of Multibody, Large Deformation Frictional Contact Problems," *Intern. J. Numer. Meth. Engng.*, Vol. 36, No. 20, pp. 3451–3485, 1993.
388. T. A. Laursen and S. Govindjee, "A note on the treatment of frictionless contact between nonsmooth surfaces in fully nonlinear problems," *Commun. Numer. Meth. Engng.*, Vol. 10, No. 11, pp. 869–878, 1994.
389. T. A. Laursen and V. G. Oancea, "Automation and Assessment of Augmented Lagrangian Algorithms for Frictional Contact Problems," *Trans. ASME, J. Appl. Mech.*, Vol. 61, No. 4, pp. 956–963, 1994.
390. T. A. Laursen, "The Convected Description in Large Deformation Frictional Contact Problems," *Intern. J. Solids and Structures*, Vol. 31, No. 5, pp. 669–681, 1994.
391. T. A. Laursen, "Nonlinear Equation Solving in the Presence of Frictional Contact Constraints," *Developments in Theoretical and Applied Mechanics / Eds. I. C. Jong and F. A. Akl*, Vol. 17, pp. 245–255, Univ. of Arkansas, Fayetteville, 1994.
392. T. A. Laursen and B. N. Maker, "An Augmented Lagrangian Quasi-Newton Solver for Constrained Nonlinear Finite Element Applications," *Intern. J. Numer. Meth. Engng.*, Vol. 38, No. 21, pp. 3571–3590, 1995.
393. T. A. Laursen, "Review of Computational Methods in Contact Mechanics," *American Scientist*, Vol. 83, pp. 196–198, 1995.
394. T. A. Laursen and V. G. Oancea, "On the Constitutive Modeling and Finite Element Computation of Rate Dependent Frictional Sliding in Large Deformations," *Comput. Meth. Appl. Mech. Engng.*, Vol. 143, No. 3–4, pp. 197–227, 1997.
395. T. A. Laursen, "On the development of thermodynamically consistent algorithms for thermomechanical frictional contact," *Comput. Meth. Appl. Mech. Engng.*, Vol. 177, No. 3–4, pp. 273–287, 1999.
396. T. A. Laursen and X. N. Meng, "A New Solution Procedure for Application of Energy-Conserving Algorithms to General Constitutive Models in Nonlinear Elastodynamics," *Comput. Meth. Appl. Mech. Engng.*, Vol. 190, No. 5, pp. 6309–6322, 2001.
397. T. A. Laursen, *Computational Contact and Impact Mechanics*, Springer, Heidelberg, 2002.

398. T. A. Laursen and G. R. Love, "Improved Implicit Integrators for Transient Impact Problems - Geometric Admissibility Within the Conserving Framework," *Intern. J. Numer. Meth. Engng*, Vol. 53, No. 2, pp. 245–274, 2002.
399. B. C. Lee and B. M. Kwak, "A computational method for elasto-plastic contact problems," *Computers and Structures*, Vol. 18, No. 5, pp. 757–765, 1984.
400. C. Y. Lee, J. T. Oden, M. Ainsworth, "Local a posteriori error estimates and numerical results for contact problems and problems of flow through porous media," *Nonlinear Computational Mechanics / Eds. P. Wriggers and W. Wagner*. pp. 671–689, Springer, Berlin, 1991.
401. C. Y. Lee and J. T. Oden, "A priori error estimation of hp-finite element approximations of frictional contact problems with normal compliance," *Intern. J. Engng. Sci.*, Vol. 31, No. 6, pp. 927–952, 1993.
402. C. Y. Lee and J. T. Oden, "Theory and approximation of quasi-static frictional contact problems," *Comput. Meth. Appl. Mech. Engng*, Vol. 106, No. 3, pp. 407–429. 1993.
403. C. Y. Lee and J. T. Oden, "A-posteriori error estimation of hp finite-element approximations of frictional contact problems," *Comput. Meth. Appl. Mech. Engng*, Vol. 113, No. 1–2, pp. 11–45, 1994.
404. J. Lemaitre *A course on Damage Mechanics*. Springer, Berlin, 1992.
405. J. Lemaitre *A course on Damage Mechanics*. Springer, Berlin, 1996.
406. J. P. Lewis, M. Cordner, N. Fong, "Pose space deformation: a unified approach to shape interpolation and skeleton-driven deformation," *Proc. SIGGRAPH 2000, Annual Conf. Series*, pp. 165–172, 2000.
407. L. Li and P. Bettess, "Adaptive finite element methods: A review," *AMR*, Vol. 50, No. 10, pp. 581–591, 1997.
408. S. Li and W. K. Liu, "Meshfree and particle methods and their applications," *AMR*, Vol. 55, No. 1, pp. 1–34, 2002.
409. W. Ling and H. K. Stolarski, "On elasto-plastic finite element analysis of some frictional problems with large sliding," *Engng. Computations*, Vol. 14, No. 5, pp. 558–580, 1997.
410. J.-L. Lions, "The work of Stampacchia in variational inequalities," in *Variational Inequalities and Complementarity Problems: Proc. Intern. School*, pp. 1–24, 1978.
411. V. D. Liseikin and N. N. Yanenko, "Moving coordinate method in gas dynamics," *Chislennye Metody v Mekhanike Sploshnykh Sred*, Vol. 7, No. 2, pp. 75–82, 1976.
412. V. D. Liseikin, *Grid Generation Methods*, Springer-Verlag, New-York, 1999.
413. W. K. Liu, S. Jun, Y. F. Zhang, "Reproducing Kernel Particle Methods," *Intern. J. Numer. Meth. Fluids*, Vol. 20, pp. 1081–1106, 1995.
414. W. K. Liu, Y. Chen, R. A. Uras, C. T. Chang, "Generalized Multiple Scale Reproducing Kernel Particle Methods," *Comput. Meth. Appl. Mech. Engng*, Vol. 139, pp. 91–158, 1996.
415. N. Lock, M. Jaeger, M. Medale, and R. Occelli, "Local mesh adaptation technique for front tracking problems," *Int. J. Numer. Methods Fluids*, Vol. 28, p. 719, 1998.
416. G. Maenchen and S. Sack, "The TENSOR code," in *Methods in Computational Physics. Vol. 3. Fundamental methods in Hydrodynamics*. pp. 181–210, Acad. Press, N.Y., 1964.
417. J. G. Malone, "Automated mesh decomposition and concurrent finite element analysis for hypercube multiprocessor computer," *Comput. Meth. Appl. Mech. Engng*, Vol. 70, No. 1, pp. 27–58, 1988.
418. J. G. Malone and N. L. Johnson, "A parallel finite element contact impact algorithm for non-linear explicit transient analysis: Part I - The search algorithm and contact mechanics," *Intern. J. Numer. Meth. Engng*, Vol. 37, No. 4, pp. 559–590, 1994.
419. J. G. Malone and N. L. Johnson, "A parallel finite element contact impact algorithm for non-linear explicit transient analysis: Part II - Parallel implementation," *Intern. J. Numer. Meth. Engng*, Vol. 37, No. 4, pp. 591–603, 1994.
420. A. V. Manzhirov, "Contact problems for non-homogeneous aging bodies," in *Mechanics of Contact Interaction [in Russian]*, I. I. Vorovich and V. M. Alexandrov (eds.), pp. 549–565, Fizmatlit, Moscow, 2001.

421. A. V. Manzhairov, "Contact problems of mechanics of accreting bodies," in *Mechanics of Contact Interaction* [in Russian], I. I. Vorovich and V. M. Alexandrov (eds.), pp. 607–621, Fizmatlit, Moscow, 2001.
422. W. R. Marks and N. J. Salamon, "A projected conjugate gradient method for frictionless contact problems." *Trans. ASME. J. Vibrations, Acoustics, Stress and Reliability in Design*, Vol. 105, 1983.
423. J. A. C. Martins and J. T. Oden, "Existence and uniqueness results for dynamic contact problems with nonlinear normal and friction interface laws," *Nonlinear Analysis Theory Methods and Applications*, Vol. 11, No. 3, pp. 407–428, 1987.
424. F. Mashayek and N. Ashgriz, "A hybrid finite-element-volume-of-fluid method for simulating free surface flows and interfaces," *Int. J. Numer. Methods Fluids*, Vol. 20, p. 1363, 1995.
425. H.-O. May, "The conjugate gradient method for unilateral problems," *Comput. Meth. Appl. Mech. Engng*, Vol. 12, No. 4, pp. 595–598, 1986.
426. T. W. McDevitt and T. A. Laursen, "A Mortar-Finite Element Formulation for Frictional Contact Problems," *Intern. J. Numer. Meth. Engng*, Vol. 48, pp. 1525–1547, 2000.
427. W. H. McMaster, *Computer Codes for Fluid-Structure Interactions*, Lawrence Livermore Laboratory Report N. UCRL-89724. 1984.
428. C. Meider, *Numerical Simulation of Detonation* [Russian translation], Mir, Moscow, 1985.
429. J. M. Melenk and I. Babuska, "The Partition of Unity Finite Element Method: Basic Theory and Applications," *Comput. Meth. Appl. Mech. Engng*, Vol. 139, No. 1–4, pp. 289–314, 1996.
430. N. G. Meleshchenko, "To the design evaluation of operating conditions of butt-joints in engines," in *Transactions of Diesel Research Institute* [in Russian], Issue 73, pp. 31–36, 1978.
431. G. P. Men'shikov, V. A. Odintsov, and L. A. Chudov, "Indentation of a cylindrical impactor into a finite plate," *Izv. AN SSSR. MTT [Mechanics of Solids]*, No. 1, pp. 125–130, 1976.
432. L. A. Merzhevskii and A. D. Ressiyanskii, "Numerical simulation of break-through of obstacles by a cylindrical projectile," in *Mechanics of Transient Processes* [in Russian], Novosibirsk, 1984, pp. 86–91.
433. R. Michalowski and Z. Mroz, "Associated and nonassociated sliding rules in contact friction problems," *Arch. Mech.*, Vol. 30, No. 3, pp. 259–276, 1978.
434. A. Mikolajczak, A. Rassineux, F. Dufossi, V. Kromer, "A finite element procedure of contact problems based on a remeshing of the contact zone," in *European Congr. on Comput. Methods in Appl. Sci. Engng*. pp. 1-15, ECCOMAS. Barcelona, 2000.
435. K. Miller, K. Chinzei, G. Orssengo, P. Bednarz, "Mechanical properties of brain tissue in-vivo: experiment and computer simulation," *J. Biomechanics*, Vol. 33, No. 11, pp. 1369–1376, 2000.
436. H. Miyata, "Finite difference simulation of breaking waves," *J. Comput. Phys.*, Vol. 65, pp. 179–214, 1986.
437. N. Moes, J. Dolbow, T. Belytschko, "A finite element method for crack growth without remeshing," *Intern. J. Numer. Methods Engng*, Vol. 46, pp. 131–150, 1999.
438. J. J. Monaghan, "Why Particle Methods Work," *SIAM Journal Sci. Stat. Comput.*, Vol. 3, No. 4, pp. 422–433, 1982.
439. Moresi L., Muhlhaus H., Dufour F. An overview of numerical methods for Earth simulations. 2001. Internet:
Internet: www.ned.dem.csiro.au/research/solidMech/Geodynamics/ChapmanConference/AbstractsReceived/AbstractFiles/Moresi-et-al.pdf
440. E. M. Morozov and G. P. Nikishkov, *Finite Elements in Fracture Mechanics* [in Russian], Nauka, Moscow, 1980.
441. N. F. Morozov, V. I. Smirnov, and Yu. V. Petrov, "On the erosion damage of solids," in *Mechanics of Contact Interaction* [in Russian], I. I. Vorovich and V. M. Alexandrov (eds.), pp. 640–650, Fizmatlit, Moscow, 2001.
442. A. Munjiza, D. E. Owen, N. Bicanic, "A Combined Finite-Discrete Element Method in Transient Dynamics of Fracturing Solids," *Eng. Computations*, Vol. 12, pp. 145–174, 1995.

443. B. Nichols, "Further development of the marker-and-cell method for incompressible fluid flow," in *Numerical Methods in Fluid Mechanics* [Russian translation], O. M. Belotserkovskii (ed.), pp. 165–173, Mir, Moscow, 1973.
444. B. D. Nichols and C. W. Hirt, "Methods for Calculating Multi-Dimensional, Transient Free Surface Flows Past Bodies," *Proc. 1st Intern. Conf. Num. Ship Hydrodynamics*. Gaithersburg, 1975.
445. R. I. Nigmatulin, *Dynamics of Multi-phase Media* [in Russian], Nauka, Moscow, 1987.
446. I. S. Nikitin, *Dynamics of Laminated Beam Media with Slip and Friction* [in Russian], Preprint No. 366, Institute for Problems in Mechanics of the USSR Academy of Sciences, Moscow, 1989.
447. G. P. Nikishkov and V. G. Pashnin, "Calculation of stress states in contacting bodies with the use of isoparametric contact elements," in *Strength of Materials and Structural Members of Nuclear Reactors* [in Russian], Energoatomizdat, Moscow, 1985.
448. G. P. Nikishkov, *Software Complex for Solving Problems in Solid Mechanics* [in Russian], MIFI, Moscow, 1988.
449. V. F. Noh, "Combined Eulerian-Lagrangian (CEL(??)) method for unsteady 2D problems," in *Numerical Methods in Hydrodynamics* [Russian translation], Mir, Moscow, 1967.
450. B. Nour-Omid and P. Wriggers, "A 2-level iteration method for solution of contact problems," *Comput. Meth. Appl. Mech. Engng*, Vol. 54, No. 2, pp. 131–144, 1986.
451. J. T. Oden and E. B. Pires, "Algorithms and numerical results for finite-element approximations of contact problems with non-classical friction laws," *Computers and Structures*, Vol. 19, No. 1–2, pp. 137–147, 1983.
452. J. T. Oden, J. A. C. Martins, "Models and computational methods for dynamic frictional phenomena" *Comput. Meth. Appl. Mech. Engng*. Vol. 52. pp. 527–634, 1986.
453. A. Oishi, Large-scale dynamic analyses with contact-impact using the hierarchical domain decomposition method, Annual report of Adventure Project ADV-99-1. Tokushima. pp. 1–23, 1999.
454. M. Okrouhlik, "Mechanics of contact impact," *AMR*. Vol. 47, No. 2, pp. 33–99, 1994.
455. M. Oldenburg and L. Nilsson, "The position code algorithm for contact searching," *Intern. J. Numer. Meth. Engng*, Vol. 37, pp. 359–386, 1994.
456. O. A. Oleinik, "On one method for solving the Stephan problem in the general case," *Doklady AN SSSR*, Vol. 135, No. 5, pp. 1054–1057, 1960.
457. J. Oliver, M. Cervera, O. Manzoli, "On the use of strain-softening models for the simulation of strong discontinuities in solids," in *Material instabilities in solids*, pp. 107–123, Wiley, Chichester, 1998.
458. E. Onate, S. R. Idelsohn, O. C. Zienkiewicz, and R. L. Taylor, "A finite point method in computational mechanics. Applications to convective transport and fluid flow," *Intern. J. Numer. Meth. Engng*, Vol. 39, pp. 3839–3866, 1996.
459. E. Onate, S. R. Idelsohn, F. Del Pin, R. Aubry, "The particle finite element method. An overview," *Intern. J. Comput. Meth.*, Vol. 1, No. 2, pp. 267–307, 2004.
460. E. S. Oran and J. P. Boris, *Numerical Simulation of Reactive Flow*, Elsevier, New York, 1987.
461. S. Osher and J. A. Sethian, "Front propagating with curvature-dependent speed: Algorithms based on Hamilton-Jacobi formulations," *J. Comput. Phys.*, Vol. 79, pp. 12, 1988.
462. S. Osher and R. Fedkiw "Level Set Methods: An Overview and Some Recent Results," *J. Comput. Phys.*, Vol. 169, No. 2, pp. 463–502, 2001.
463. S. J. Osher and G. Tryggvason, "Preface," *J. Comput. Phys.* (Special issue of JCP on methods for multiphase flows), Vol. 169, No. 2, pp. 249–249, 2001.
464. S. Osher and R. Fedkiw, *The Level Set Method and Dynamic Implicit Surfaces*, New York: Springer, 2002.
465. V. Padmanabhan and T. A. Laursen, "A Framework for Development of Surface Smoothing Procedures in Large Deformation Frictional Contact Analysis," *Finite Elements in Analysis and Design*. Vol. 37, No. 3, pp. 173–198, 2001.

466. J. Padovan, V. Tovichakohaikubs, I. Zeid, "Finite element analysis of steadily moving contact fields," *Computers and Structures*, Vol. 18, pp. 111–200, 1984.
467. J. Padovan, "Finite element analysis of steadily and transiently moving and rolling viscoelastic structure-1. Theory," *Computers and Structures*, Vol. 27, No. 2, pp. 249–257, 1987.
468. J. Padovan and P. Padovan, "Modelling wear at intermittently slipping high speed interfaces," *Computers and Structures*, Vol. 52, No. 4, pp. 795–812, 1994.
469. P. D. Panagiotopoulos, *Inequality Problems in Mechanics and Applications*. Birkhauser, Boston, 1985.
470. P. Pandolfi, C. Kane, J. E. Marsden, M. Ortiz, "Time-Discretized Variational Formulation of Nonsmooth Frictional Contact," *Intern. J. Numer. Meth. Engng*, Vol. 53, No. 8, pp. 1801–1829, 2002.
471. M. Papadrakakis and P. Ghionis "Conjugate gradient algorithms in nonlinear structural analysis problems," *Comput. Meth. Appl. Mech. Engng*, Vol. 59, pp. 11–27, 1986.
472. P. Papadopoulos and R. L. Taylor, "A Simple Algorithm for Three-dimensional Finite Element Analysis of Contact Problems," *Computers and Structures*, Vol. 46, No. 6, pp. 1107–1118, 1993.
473. H. Parisch, "A consistent tangent stiffness matrix for three-dimensional non-linear contact analysis," *Intern. J. Numer. Meth. Engng.*, Vol. 28, No. 8, pp. 1803–1812, 1989.
474. H. Parisch and Ch. Lubbing, "Formulation of arbitrary shaped surface elements for 3D large deformations contact with friction," *Intern. J. Numer. Meth. Engng*, Vol. 40, No. 18, pp. 3359–3383, 1997.
475. J. Park and W. J. Anderson, "Geometric Optimization in Presence of Contact Singularities," *AIAA J.*, Vol. 33, No. 8, pp. 1503–1509, 1995.
476. K. C. Park and C. A. Felippa, "A variational framework for solution method development in structural mechanics," *J. Appl. Mech.*, Vol. 65, No. 1, pp. 242–249, 1998.
477. K. C. Park and C. A. Felippa, "A variational principle for the formulation of partitioned structural systems," *Intern. J. Numer. Meth. Engng*, Vol. 47, No. 1–3, pp. 395–418, 2000.
478. K. C. Park, U. Gumaste, C. A. Felippa, "A localized version of the method of Lagrange multipliers and its applications," *J. Comput. Mech.*, Vol. 24, No. 6, pp. 476–490, 2000.
479. K. C. Park, C. A. Felippa, G. Rebel, "A simple algorithm for localized construction of nonmatching structural interfaces," *Intern. J. Numer. Meth. Engng*, Vol. 53, No. 9, pp. 2117–2142, 2002.
480. V. G. Pashnin and V. T. Sapunov, "Contact interaction of the fuel core with the shell of the fuel element," in *Deformation and Fracture of Materials and Structural Members of Nuclear Power Plants [in Russian]*, pp. 38–47, MIFI, Moscow, 1993.
481. J. R. Pasta and S. Ulam, "Heuristic numerical work in some problems of hydrodynamics," *Math. Tables Aids Comput.*, Vol. 13, 1959.
482. D. Peric and D. R. J. Owen, "Computational model for 3-d contact problems with friction based on the penalty method," *Intern. J. Numer. Meth. Engng*, Vol. 35, No. 6, pp. 1289–1309, 1992.
483. A. P. Peskin and G. R. Hardin, "Moving Particles Through a Finite Element Mesh," *J. Research of the National Institute of Standards and Technology*, Vol. 103, No. 1, pp. 77–93, 1998.
484. E. Petocz and F. Armero, "A Sorting Contact Detection Algorithm: Formulation and Finite Element Implementation," *UCB/SEMM Report 98/06*. Univ. California, Berkeley, 1998.
485. I. B. Petrov and A. S. Kholodov, "Numerical study of some dynamic problems of solid mechanics by means of the grid-characteristic method," *Zhurnal Vychislitel'noi Matematiki i Matematicheskoi Fiziki [Journal of Computational Mathematics and Mathematical Physics]*, Vol. 24, No. 5, pp. 722–739, 1984.
486. F. Pfeiffer, "Unilateral problems of dynamics," *Archive of Applied Mechanics*, Vol. 69, No. 8, pp. 503–527, 1999.
487. G. Pietrzak and A. Curnier, "Continuum mechanics modelling and augmented lagrangian formulation of multibody, large deformation frictional contact problems," in *Comput. Plasticity, Fundamentals and Applications*, Ed. D. R. J. Owen et al., pp. 878–883. CIMNE, Barcelona, 1997.
488. A. B. Pifco and R. Winter "Theory and application of finite element analysis to structural crash simulation," *Computers and Structures*, Vol. 13, pp. 277–285, 1981.

489. E. B. Pires and J. T. Oden, "Analysis of contact problems with friction under oscillating loads," *Comput. Meth. Appl. Mech. Engng*, Vol. 39, No. 3, pp. 337–362, 1983.
490. S. Plimpton, S. Attaway, B. Hendrickson, et al., "Transient Dynamics Simulations: Parallel Algorithms for Contact Detection and Smoothed Particle Hydrodynamics," *J. Parallel and Distributed Computing*, Vol. 50, pp. 104–122, 1998.
Internet: <http://www.cs.sandia.gov/~sjplimp/main.html>
491. A. M. Podgorny, P. P. Gontarovskii, G. A. Marchenko, and V. N. Terlin, *Some Applied Mixed-type Problems of Elastoplasticity* [in Russian], Preprint No. 36, Institute of Problems of Mechanical Engineering, Kharkov, 1976.
492. A. M. Podgorny, P. P. Gontarovskii, B. N. Kirkach, et al., *Problems of Contact Interaction of Structural Members* [in Russian], V. L. Rvachev (ed.), Naukova Dumka, Kiev, 1989.
493. V. A. Postnov and I. Ya. Kharkhurim, *Finite Element Method for the Design of Ship Structures* [in Russian], Sudostroenie, Leningrad, 1974.
494. D. Potter, *Numerical Methods in Physics* [Russian translation], Mir, Moscow, 1975.
495. A. A. Pozdeev, P. V. Trusov, and Yu. I. Nyashin, *Large Elastoplastic Deformations* [in Russian], Nauka, Moscow, 1986.
496. E. J. Praskacz "On impact-contact algorithms for parallel distributed-memory computers," in *Computational Mech. '95. Proc. Intern. Conf. Comput. Engng. Science.*, pp. 369–374, Hawaii, USA, 1995.
497. B. N. Pshenichnyi and Yu. M. Danilin, *Numerical Methods in Extremum Problems* [in Russian], Nauka, Moscow, 1975.
498. E. G. Puckett and J. S. Saltzman, "A 3D adaptive mesh refinement algorithm for multimaterial gas dynamics," *Physica*, Vol. D60, p. 84, 1992.
499. E. G. Puckett, A. S. Almgren, J. B. Bell, D. L. Marcus, W. J. Rider, "A high-order projection method for tracking fluid interfaces in variable density incompressible flows," *J. Comput. Phys.*, Vol. 130, p. 269, 1997.
500. M. A. Puso and T. A. Laursen, "A 3D Contact Smoothing Method Using Gregory Patches," *Intern. J. Numer. Meth. Engng*, Vol. 54, No. 8, pp. 1161–1194, 2002.
501. P. J. Rabier, J. A. C. Martins, T. J. Oden, L. Campos, "Existence and local uniqueness of solutions to contact problems in elasticity with nonlinear friction laws," *Intern. J. Engng. Sci.*, Vol. 24, No. 11, pp. 1755–1768, 1986.
502. P. J. Rabier and J. T. Oden, "Solution to Signorini-like contact problems through interface models. 1. Preliminaries and formulation of a variational equality," *Nonlinear Analysis Theory Methods and Applications*, Vol. 11, No. 12, pp. 1325–1350, 1987.
503. P. J. Rabier and J. T. Oden, "Solution to Signorini-like contact problems through interface models. 2. Existence and uniqueness theorems," *Nonlinear Analysis Theory Methods and Applications*, Vol. 12, No. 1, pp. 1–17, 1988.
504. M. Raous and S. Barbarin, "Conjugate Gradient for Frictional Contact," in *Proc. Contact Mechanics Intern. Symp. / Ed. A. Curnier*, pp. 123–132, Presses Polytech. et Univ. Romandes, Lausanne, 1992.
505. M. Raous and S. Barbarin, "Stress waves in a sliding contact - Part 2: Modeling," in *Proc. 22nd Leeds-Lion Symposium on Tribology / Eds. D. Dowson et al. Tribology Series. Vol. 31. Amsterdam: Elsevier*, 1996.
506. M. M. Rashid, "The arbitrary local mesh refinement method: an alternative to remeshing for crack propagation analysis," *Comput. Meth. Appl. Mech. Engng*, Vol. 154, No. 1–2, pp. 133–150, 1998.
507. G. Rebel, K. C. Park, C. A. Felippa, "A contact-impact formulation based on localized Lagrange multipliers," *Center for Aerospace Structures. Report No. CU-CAS-00-18. Univ. Colorado, Boulder*, 2000.

508. A. D. Resnyanskii and L. A. Merzhievskii, "Application of the moving grid method to problems of fracture of solids," in *Dynamics of a Continuous Medium* [in Russian], Institute of Hydrodynamics of the Siberian Branch of the Russian Academy of Sciences, Novosibirsk, Issue 66, pp. 150–157, 1984.
509. W. J. Rider and D. B. Kothe, "Stretching and Tearing Interface Tracking Methods," Technical Report AIAA – 95-0699, AIAA, 1995.
Internet: www.c3.lanl.gov/~wjr/publ.html).
510. W. J. Rider and D. B. Kothe, "Reconstructing Volume Tracking," *J. Comput. Phys.*, Vol. 141, pp. 112–152, 1998.
511. B. E. Ringers, "New sliding surface techniques enable lagrangian code to handle deep target penetration/perforation problems," *Lect. Notes Engng*, No. 3, pp. 36–46, 1983.
512. G. Rodrigue (ed.), *Parallel Computations* [Russian translation], Nauka, Moscow, 1986.
513. A. A. Rogovoi, "Variational statement of the elastoplastic problem for large deformations in terms of Eulerian-Lagrangian coordinates," in *Stresses and strains in Structures and Materials* [in Russian], Urals Scientific Center of the USSR Academy of Sciences, Sverdlovsk, 1985, pp. 77–83.
514. L. A. Rozin, *Computer-aided Design of Hydraulic Structures. Finite Element Method* [in Russian], Energiya, Moscow, 1971.
515. L. A. Rozin, *Finite Element Method for Elastic Systems* [in Russian], Stroiizdat, Moscow, 1977.
516. L. A. Rozin and M. S. Smirnov, "Solution of contact problems of elasticity with compliances in unilateral constraints," *Izv. Vuzov. Stroitel'stvo*, No. 5, pp. 27–32, 2000.
517. A. I. Ruzanov, L. K. Romanycheva, and I. A. Volkov, "Construction of numerical models and numerical analysis of fracture in solids subjected to an impulsive load," in *Mechanics of Transient Processes* [in Russian], pp. 98–105, Institute of Hydrodynamics of the Siberian Branch of the Russian Academy of Sciences, Novosibirsk, 1984.
518. V. L. Rvachev, *R-functions: Theory and some Applications* [in Russian], Naukova Dumka, Kiev, 1982.
519. V. L. Rvachev and T. I. Sheiko, "R-functions in boundary value problems in mechanics," *AMR*, Vol. 48, No. 4, pp. 151–188, 1995.
520. O. M. Sadovskaya, "On the numerical formulation of dynamic contact interaction conditions with friction being taken into account," in *Theory of Grid Methods for Solving Boundary-value Problems, Materials of the 2nd All-Russian Seminar* [in Russian], pp. 63–64, Unipress, Kazan, 1998.
521. O. M. Sadovskaya, "On the numerical analysis of an impact of elastoplastic bodies with finite rotations being taken into account," in *Dynamics of a Continuous Medium. Mathematical Problems of Mechanics of a Continuous Medium* [in Russian], Issue 114, pp. 196–199, Institute of Hydrodynamics, Novosibirsk, 1999.
522. O. M. Sadovskaya, "Numerical solution of dynamic contact problems," in *Materials of the Conference of Young Scientists* [in Russian], pp. 42–54, Institute of Computational Mathematics, Siberian Branch of Russian Academy of Sci., Krasnoyarsk, 1999.
523. V. M. Sadovskii, "Hyperbolic variational inequalities in dynamics of elastoplastic bodies," *PMM [Applied Mathematics and Mechanics]*, Vol. 55, No. 6, pp. 1041–1048, 1991.
524. V. M. Sadovskii, *Discontinuous Solutions in Dynamics of Elastoplastic Media* [in Russian], Nauka, Fizmatlit, Moscow, 1997.
525. A. I. Sadyrin, "To the determination of contact forces in the case of an impact of elastoplastic bodies," in *Applied Problems of Strength and Plasticity* [in Russian], Issue 3, pp. 70–73, Gor'kovskii Universitet, Gorky, 1976.
526. A. I. Sadyrin, "Finite-difference approximation of boundary conditions in a dynamic contact problem," in *Applied Problems of Strength and Plasticity* [in Russian], Issue 13, pp. 51–56, Gor'kovskii Universitet, Gorky, 1979.
527. A. I. Sadyrin, "Simulation of dynamic fracture of solids in the case of impact contact interaction," in *Applied Problems of Strength and Plasticity* [in Russian], Issue 53, pp. 132–141, TNI KMK, Moscow, 1995.

528. A. Ya. Sagomonyan, *Obstacle Break-through Dynamics* [in Russian], Izd-vo MGU, Moscow, 1988.
529. A. F. Saleeb, K. Chen, T. Y. P. Chang, "An effective two-dimensional frictional contact model for arbitrary curved geometry," *Intern. J. Numer. Meth. Engng*, Vol. 37, No. 8, pp. 1297–1321, 1994.
530. A. Santos and A. Makinouchi, *J. Mater. Proc. Tech.*, Vol. 50, p. 277, 1993.
531. A. A. Samarskii and B. D. Moiseenko, "An efficient through-calculation scheme for multidimensional Stephan's problem," *Zhurnal Vychislitel'noi Matematiki i Matematicheskoi Fiziki* [Journal of Computational Mathematics and Mathematical Physics], Vol. 5, No. 5, pp. 816–827, 1965.
532. M. S. Samigulin, Yu. V. Yanilkin, E. S. Gavrilova, and A. A. Shanin, "A method for numerical simulation of 2D flows of dispersed media in continuous approximation," *VANT. Ser. MMFP. Issue 1*, pp. 3–8, 1995.
533. V. V. Sazhin and I. V. Simonov, *An Impact of Elastic and Elastoplastic Rectangles at Small Angle* [in Russian], Preprint No. 300, Institute for Problems in Mechanics of the USSR Academy of Sciences, Moscow, 1987.
534. T. W. Sederberg, S. R. Parry, "Free-Form deformation of solid geometry models," *Computer Graphics (Siggraph)* vol. 20, No. 4, pp. 151–160, 1996.
535. A. A. Seireg and J. Rodriguez, *Optimizing the Shape of Mechanical Elements and Structures*, Dekker, New York, 1997.
536. J. A. Sethian, *Level Set Methods. Evolving Interfaces in Geometry, Fluid Mechanics, Computer Vision, and Materials Science*, Cambridge Univ. Press, Cambridge, England, 1996.
537. J. A. Sethian, "Tracking interfaces with level sets," *American Scientist*, Vol. 85, p. 254, 1998.
538. J. A. Sethian, *Level Set Methods and Fast Marching Methods: Evolving Interfaces in Computational Geometry, Fluid Mechanics, Computer Vision, and Materials Science*. Cambridge Univ. Press, Cambridge, England, 1999.
539. J. Sethian, "Evolution, Implementation, and Application of Level Set and Fast Marching Methods for Advancing Fronts," *J. Comput. Phys.*, Vol. 169, No. 2, pp. 503–555, 2001.
540. I. Shai and M. Santo, "Heat transfer with contact resistance," *Intern. J. Heat Mass Transfer*, Vol. 24, pp. 465–470, 1982.
541. N. H. Sharif and N.-E. Wiberg, "Stationary level set method for modeling sharp interfaces in ground-water flow," Preprint No. 2001:06, Chalmers University, Goteborg, 2001.
Internet: www.phi.chalmers.se/pub/preprints/pdf/phiprint-2001-06.pdf
542. Yu. N. Shevchenko, V. V. Piskun, and V. G. Savchenko, *Solution of the Axially Symmetric 3D Problem of Thermoplasticity on M-220-type Computers* [in Russian], Naukova Dumka, Kiev, 1975.
543. W. Shyy, M. Francois, H. S. Udaykumar, et al., "Moving boundaries in micro-scale biofluid dynamics," *AMR*, Vol. 54, No. 5, pp. 405–453, 2001.
544. A. Signorini, "Sopra alcune questione di elastostatica," *Atti Soc. Ital. Progr. Sci.*, pp. 513–533, 1933.
545. A. Signorini, "Questioni di elasticitanon linearizzata o semilinearizzat e semilinearizzata," *Rend. di Matem. e delle sue appl.*, Vol. 18, No. 1–2, pp. 95–139, 1959.
546. Simo J.C., Wriggers P., Taylor R.L. *A Perturbed Lagrangian Formulation for the Finite-element Solution of Contact Problems // Comput. Meth. Appl. Mech. Engng.* 1985. V. 50. P. 163-180.
547. J. C. Simo, P. Wriggers, K. H. Schweizerhof, R. L. Taylor, "Finite deformation post-buckling analysis involving inelasticity and contact constraints," *Intern. J. Numer. Meth. Engng*, 1986, Vol. 23, pp. 779–800, 1986.
548. J. C. Simo and T. A. Laursen, "An augmented lagrangian treatment of contact problems involving friction," *Computer and Structures*, Vol. 42, No. 1, pp. 97–116, 1992.
549. J. Simo, J. Oliver, F. Armero, "An analysis of strong discontinuities induced by softening solutions in rate-independent solids," *J. Comput. Mech.*, Vol. 12, No. 5, pp. 277–296, 1993.
550. I. V. Simonov, "Contact problems of wedging of elastic bodies," in *Mechanics of Contact Interaction* [in Russian], I. I. Vorovich and V. M. Alexandrov (eds.), pp. 654–667, Fizmatlit, Moscow, 2001.

551. J. W. Simons and P. G. Bergan, "A finite element formulation of three-dimensional contact problems with slip and friction," *J. Comput. Mech.*, Vol. 1, No. 2, pp. 153–164, 1986.
552. D. B. Spalding and L. Jun, "Numerical simulation of flows with moving interfaces," *PhysicoChemical Hydrodynamics*, Vol. 10, No. 5/6, pp. 625–637, 1988.
553. A. L. Stadnik, A. A. Shanin, and Yu. V. Yanilkin, "Eulerian technique TREK(?) for the calculation of 3D multi-component dynamic gas flows," *VANT. Ser. MMFP. Issue 4*, pp. 71–78, 1994.
554. A. L. Stadnik, V I Tarasov, and Yu. V. Yanilkin, "Eulerian technique for the calculation of 3D multi-component elastoplastic flows," *VANT. Ser. MMFP. Issue 3*, pp. 52–60, 1995.
555. J. T. Stadter and R. O. Weiss, "Analysis of Contact through Finite Element Gaps," *Computers and Structures*, Vol. 10. pp. 867–873, 1979.
556. G. Stampacchia and J. L. Lions, "Inequations variationnelles non coercives," *C. R. Acad. Sci.*, Vol. 261, No. 1, pp. 25–27, 1965.
557. G. Stampacchia and J. L. Lions, "Variational inequalities," *Commun. Pure Appl. Math.*, Vol. 20, pp. 493–519, 1967.
558. G. Streng and J. Fix, *Theory of the Finite Element Method [Russian translation]*, Mir, Moscow, 1977.
559. Y. Sumi, "Computational crack path prediction," *Theoret. Appl. Fract. Mech.*, Vol. 4, pp. 149–156, 1985.
560. S. M. Sun, H. S. Tzou, M. C. Natori, "Parametric quadratic programming method for dynamic contact problems with friction," *AIAA J.*, Vol. 32, No. 2, pp. 371–378, 1994.
561. M. Sussman, P. Smereka, S. Osher, "A level set approach for computing solutions to incompressible two-phase flow," *J. Comput. Phys.*, Vol. 114, No. 1, p. 146, 1994.
562. M. Sussman, et al., "An adaptive level set approach for incompressible two-phase flows," *J. Comput. Phys.*, Vol. 148, No. 1, pp. 81–124, 1999.
563. P. Szabo and O. Hassager, "Simulation of free surfaces in 3-d with the arbitrary Lagrange-Euler method," *Int. J. Num. Meth. Engng*, Vol. 38, pp. 717–734, 1995.
564. W. G. Szymczak, J. C. W. Rogers, J. M. Solomon, A. E. Berger, "A numerical algorithm for hydrodynamic free boundary problems," *J. Comput. Phys.*, Vol. 106, pp. 319–336, 1993.
565. Y. Tada and N. Nishihara, "Optimum Shape Design of Contact Surface with Finite Element Methods," *Advances in Engineering Software*, Vol. 18, pp. 75–85, 1993.
566. D. Tabor, "Friction - The Present state of Our Understanding," *J. Lubr. Technology*, Vol. 103, pp. 169–179, 1981.
567. D. A. Tarzia, A bibliography on moving-free boundary problems for the heat-diffusion Stefan problem, Technical Report, University di Ferenze, 1988.
568. R. L. Taylor and P. Papadopoulos "On a Patch Test for Contact Problems in Two Dimensions," in *Nonlinear Computational Mechanics / Eds. P. Wriggers and W. Wagner*, P. 690-702, Springer, Berlin, 1991.
569. R. L. Taylor and P. Papadopoulos, "On a Finite Element Method for Dynamic Contact/Impact Problems," *Intern. J. Numer. Meth. Engng*, Vol. 36, pp. 2123–2140, 1993.
570. D. Terzopoulos, J. Platt, A. Barr, K. Fleischer, "Elastically deformable models," *Proc. of SIGGRAPH '87, Computer Graphics*, Vol. 21, No. 4, pp. 205–214, 1987.
571. T. G. Thomas, D. C. Leslie, J. J. R. Williams, "Free Surface Simulations Using a Conservative 3D Code," *J. Comput. Phys.*, Vol. 116, pp. 52–68, 1995.
572. E. Thompson, "Use of Pseudo-Concentrations to Follow Creeping Viscous Flows During Transient Analysis," *Intern. J. Numer. Meth. Fluids*, Vol. 6, pp. 749–761, 1986; *Proc. 3rd Intern. Conf. Numer. Meth. in Fluid Dynamics. Lecture Notes in Physics*, Vol. 18, pp. 163–173, Springer, N.Y., 1986.
573. A. I. Tolstykh, "On the condensation of nodes of difference grids during the solution and application of increased-accuracy schemes for the numerical analysis of viscous gas flows," *Zhurnal Vychislitel'noi Matematiki i Matematicheskoi Fiziki [Journal of Computational Mathematics and Mathematical Physics]*, Vol. 18, No. 1, pp. 139–153, 1978.

574. M. F. Tome and S. McKee, "GENSMAC: a computational marker-and-cell method for free surface flows in general domains," *J. Comput. Phys.*, Vol. 110, pp. 171–186, 1994.
575. M. F. Tome, A. C. Filho, J. A. Cuminato, et al., "GENSMAC3D: a numerical method for solving unsteady three-dimensional free surface flows," *Intern. J. Numer. Meth. Fluids*, Vol. 37, pp. 747–796, 2001.
576. Y. Tomita, "Simulations of plastic instabilities in solid mechanics," *AMR*, Vpl. 47, No. 6, Part 1-2, pp. 171–205, 1994.
577. Tompson J.F. et al. (Eds.) *Handbook of grid generation*, CRC Press, Boca Raton, 1999.
578. E. T. Toro, *Riemann Solvers and Numerical Methods for Fluid Dynamics*, Springer, Berlin, 1997.
579. T. A. Toporova and Yu. V. Yanilkin, "A technique for the calculation of 2D multi-component flows with the medium strength properties being taken into account," *VANT. Ser. MMFP. Issue 4*, pp. 58–66, 1994.
580. I. N. Tsvetkova, "Accuracy analysis of contact interaction algorithms for 3D problems of dynamics of elastoplastic bodies," in *Vestnik Nizhegorodskogo Universiteta*, 1995, pp. 93–95.
581. H. S. Udaykumar, R. Mittal, W. Shyy, "Computation of Solid-Liquid Phase Fronts in the Sharp Interface Limit on Fixed Grids," // *J. Comput. Phys.* 1999. V. 153. P. 535-574.
582. A. G. Ugodchikov and Yu. G. Korotkikh, *Some Methods for the Numerical Solution of Physically Nonlinear Problems of the Theory of Plates and Shells* [in Russian], Naukova Dumka, Kiev, 1967.
583. S. Ulam, "Stability in the case of calculations using the multi-body method," in *Hydrodynamic Instability* [Russian translation], Birkhoff(?), Bellman(?), and Lin(?) (eds.), Mir, Moscow, 1964.
584. S. O. Unverdi and G. Tryggvason, "A front-tracking projection method for viscous, incompressible, multi-fluid flows," *J. Comput. Phys.*, Vol. 100, No. 1, pp. 25–37, 1992.
585. R. Verfurth, "A Review of a posteriori error estimation and adaptive mesh refinement techniques," Technical report. Institut fur Angewandte Mathematik, Zurich Universitat, Zurich, 1993.
586. D. V. Vainberg, A. S. Gorodetskii, V. V. Kirichevskii, and A. S. Sakharov, "Finite-element method in mechanics of deformable bodies," *Prikladnaya Mekhanika*, Vol. 8, No. 8, pp. 3–28, 1972.
587. I. I. Vorovich and V. M. Alexandrov (editors), *Mechanics of Contact Interactions* [in Russian], Nauka, Moscow, 2001.
588. A. V. Vovkushevskii, "Variational statement and methods of solution of the contact problem with friction and surface roughness being taken into account," *Izv. AN SSSR MTT* [Mechanics of Solids], No. 3, pp. 56–62, 1991.
589. P. A. Voinovich and D. M. Sharov, "Modeling of gas discontinuous flows on unstructured grids," *Matematicheskoe Modelirovanie*, Vol. 5, No. 7, pp. 101–112, 1993.
590. S. P. Wang and E. Nakamachi, "The inside-outside search algorithm for finite element analysis," *Intern. J. Numer. Meth. Engng.*, Vol. 40, No. 19, pp. 3665–3685, 1997.
591. J. E. Welch, F. H. Harlow, J. P. Shannon, B. J. Daly, "The MAC method," Report LA-3425, Los Alamos Scientific Laboratory, 1965.
592. N. Wikstrom, "A literature survey aiming to shed some light on the cavitation simulation problem," Techn. Report, Chalmers Univ. Techn., Goteborg, 2000.
Internet: www.na.chalmers.se/~niklasw/documents/survey.pdf
593. M. L. Wilkins, "Calculation of elastic-plastic flow," in *Methods in Computational Physics. V. 3. Fundamental methods in Hydrodynamics*, pp. 211–263. Acad. Press, New York, 1964.
594. M. L. Wilkins, "Calculation of elastoplastic flows," in *Numerical Methods in Hydrodynamics* [Russian translation], B. Older (ed.), pp. 212–263, Mir, Moscow, 1967.
595. M. L. Wilkins, "Mechanics of penetration and perforation," *Intern. J. Engng. Sci.*, Vol. 16, No. 11, pp. 793–807, 1978.
596. M. L. Wilkins, "Computer simulation of penetration phenomena," in *Ballistic materials and penetration mechanics* / Ed. R. C. Laible, P. 225–252, Amsterdam, New York, Oxford, 1980.

597. M. L. Wilkins, "Use of artificial viscosity in multidimensional fluid dynamic calculations," *J. Comput. Phys.*, Vol. 36, p. 281, 1980.
598. M. L. Wilkins, *Computer Simulation of Dynamic Phenomena*. Springer, New York, 1999.
599. K. L. Woo and T. R. Thomas, "Contact of Rough Surfaces: A Review of Experimental Works," *Wear*, Vol. 58, pp. 331–340, 1980.
600. P. Wriggers, W. Wagner, E. Stein, "Algorithms for Nonlinear Contact Constraints with Application to Stability Problems of Rods and Shells," *J. Comput. Mech.*, Vol. 2, No. 3, pp. 215–230, 1987.
601. P. Wriggers, T. V. Van, E. Stein, "Finite-element formulation of large deformation impact-contact problems with friction," *Computers and Structures*, Vol. 37, No. 3, pp. 319–331, 1990.
602. P. Wriggers, "Finite Element Algorithms for Contact Problems," *Arch. Comput. Meth. Engng*, Vol. 2, p. 49, 1995.
603. P. Wriggers and O. Scherf, "Adaptive finite element techniques for frictional contact problems involving large elastic strains," *Comput. Meth. Appl. Mech. Engng*, Vol. 151, pp. 593–603, 1998.
604. P. Wriggers and P. Panagiotopoulos, *New Developments in Contact Problems*, CISM courses and lectures, No. 384, Springer, Udine, Wien, New York, 1999.
605. Wu-ting Tsai and D. K. R. Yue, "Computation of nonlinear free surface flows," *Annu. Rev. Fluid. Mech.*, Vol. 28, pp. 249–278, 1996.
606. Y. M. Xie and G. P. Steven, "A Simple Evolutionary Procedure for Structural Optimization," *Computers and Structures*, Vol. 49, No. 3, pp. 885–896, 1993.
607. Y. M. Xie and G. P. Steven, *Evolutionary Structural Optimization*. Springer, Berlin, 1997.
608. H.-L. Xing, T. Fujimoto, A. Makibouchi, G. P. Nikishkov, "Static-explicit FE modeling of 3-d large deformation multibody contact problems on parallel computer," in *Simulation of Material Processing: Theory, Methods, Applications* / Eds. Huetink and Baajiens, pp. 207–212, Balkema, Rotterdam, 1998.
609. H.-L. Xing and A. Makinouchi, "A node-to-point contact element strategy and its applications," *RIKEN Review*, No. 30, pp. 35–99, 2000.
610. T. Yabe, F. Xiao, Y. Zhang, "Strategy for unified solution of solid, liquid, gas and plasmas," *AIAA Paper No. 99-3509*, 30th AIAA Fluid Dynamics Conf., Norfolk, 1999.
611. G. Yagawa, S. Yosimura, N. Soneda, "A large scale finite element analysis using domain decomposition method on a parallel computer," *Computers and Structures*, Vol. 38, No. 5–6, pp. 615–625, 1991.
612. G. Yagawa and R. Sgiويا "Parallel finite elements on a massively parallel computer with domain decomposition," *Computing Systems Engng*, Vol. 4, pp. 495–503, 1993.
613. Yu. V. Yanilkin, A. A. Shanin, N. P. Kovalev, et al., "Software complex EGAK for the calculation of 2D flows of multi-component media," *VANT. Ser. MMFP. Issue 4*, pp. 69–75, 1993.
614. Yu. V. Yanilkin, "Numerical simulation of 2D flows of a multi-component medium with some low-scale processes being taken into account," *Fizicheskaya Mezomekhanika*, Vol. 2, No. 5, pp. 27–48, 1999.
615. D. L. Youngs, "Time dependent multi-material flow with large distortion," in *Numer. Methods for Fluid Dynamics*. / Eds. K. W. Morton and J. H. Baines. Acad. Press. 1982.
616. K. I. Zapparov and V. N. Kukudzhanov, "Solution of unsteady problems of dynamics of an elastoplastic medium by means of the movable grid method," in *Numerical Methods in Solid Mechanics* [in Russian], pp. 65–86, Computing Center of the USSR Academy of Sciences, Moscow, 1984.
617. K. I. Zapparov and V. N. Kukudzhanov, *Mathematical Modeling of Impact Interaction and Fracture of Elastoplastic Bodies* [in Russian], Preprint No. 280, Institute for Problems in Mechanics of the USSR Academy of Sciences, Moscow, 1986.
618. G. Zavarise, P. Wriggers, B. A. Schrefler, "On Augmented lagrangian Algorithms for Thermomechanical Contact Problems with Friction," *Intern. J. Numer. Meth. Engng*, Vol. 38, No. 17, pp. 2929–2949, 1995.
619. M. V. Zernin, "Problems and prospects of construction of an effective finite-element model of the oil flow in liquid-friction bearing clearances, with nonuniform distribution of temperature and surface

- strains being taken into account,” Pt. 1, Problemy Tribologii, No. 1, pp. 73-78, 1997; Pt. 1, Problemy Tribologii, No. 2, pp. 57-64, 1997.
620. M. V. Zernin, “Modeling of damage in sliding bearings with failure criteria being taken into account. Communication 2: Finite element models of flow of a lubricating liquid,” *Trenie i Iznos*, Vol. 18, No. 5, pp. 603–611, 1997.
621. M. V. Zernin and E. M. Morozov, “Mechanics of fracture of bodies in the case of contact interaction,” in *Mechanics of Contact Interactions* [in Russian], I. I. Vorovich and V. M. Alexandrov (eds.), Nauka, Fizmatlit, Moscow, 2001, pp. 624–639.
622. Q. Zhang and T. Hisada, “Analysis of fluid-structure interaction problems with structural buckling and large domain changes by ALE finite element method,” *Comput. Meth. Appl. Mech. Engng*, Vol. 190, pp. 6341–6357, 2001.
623. Z. H. Zhong, “A contact searching algorithm for general 3-D contact-impact problems,” Dissertation No. 178, Linköping Institute of Technology, Linköping, 1988.
624. Z. H. Zhong and L. Nilsson, “A contact searching algorithm for general contact problems,” *Computers and Structures*, Vol. 33, No. 1, pp. 197–209, 1989.
625. Z. H. Zhong and J. Mackerle, “Static Contact Problems - A Review,” *Engng. Comput.*, Vol. 9, pp. 3–37, 1992.
626. Z. H. Zhong, *Finite Element Procedures for Contact-impact Problems*. Oxford Univ. Press, New York, 1993.
627. Z. H. Zhong and J. Mackerle, “Contact-impact problems : A review with bibliography,” *AMR*, Vol. 47, No. 2, pp. 55–76, 1994.
628. Z. H. Zhong and L. Nilsson, “Automatic contact searching algorithm for dynamic finite element analysis,” *Computers and Structures*, Vol. 52, No. 2, pp. 187–197, 1994.
629. Z. H. Zhong and L. Nilsson, “Lagrange multiplier approach for evaluation of friction in explicit finite-element analysis,” *Commun. Numer. Methods Engng*, Vol. 10, No. 3, pp. 249–255, 1994.
630. T. Zhu and S. N. Atluri, “A Modified Collocation Method and a Penalty Formulation for Enforcing the Essential Boundary Conditions in the Element Free Galerkin Method,” *Comput. Mech.*, Vol. 21, No. 3, pp. 211–222, 1998.
631. Y. Zhuang, Real-time simulation of physically-realistic global deformations, PhD thesis. Department of Electrical Engineering and Computer Science, University of California, Berkeley, 2000.
632. O. Zienkevicz, *Finite Element Method in Engineering* [Russian translation], Mir, Moscow, 1975.
633. O. C. Zienkevicz and J. Z. Zhu, “A Simple Error Estimator and Adaptive Procedure for Practical Analysis,” *Intern. J. Numer. Meth. Engng*, Vol. 24, pp. 337–357, 1987.
634. J. A. Zukas, “Numerical simulation of impact phenomena,” in *Impact dynamics*. New York etc.: Wiley, 1982. P. 367-417.
635. J. A. Zukas, T. Nicolas, and H. F. Swift, *Impact Dynamics* [Russian translation], Mir, Moscow, 1985.

Moscow

submitted
20.05.2002